Physical Properties of Highly Organic Soils and Their Importance to Mobility Considerations

Susan Frankenstein and Michael W. Parker

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Susan Frankenstein and Michael W. Parker

U.S. Army Engineer Research and Development Center (ERDC)
Cold Regions Research and Engineering Laboratory (CRREL)
72 Lyme Road
Hanover, NH 03755-1290

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Under Project 465395, ERDC 6.2 “Boreal Aspects of Ensured Maneuver (BAEM),”
and Project 471941, “Remote Assessment of Snow Mechanical Properties”
and “Mobility in Peat and Northern Soils”
Abstract

In this report, we begin by investigating the different methods for calculating the seasonal bearing capacity of soils, including highly organic ones such as peat. First, we present the generalized plate theories, including failure criteria, for linear elastic, plastic, and modified plastic. In all instances, the plate is assumed to be uniform, circular, and of infinite extent. The physical properties that determine soil strength change with temperature, water content, and ice content. It is therefore important to accurately predict these. Therefore, we include a section on calculating the soil thermal conductivity, which determines the flow of heat. Following the discussion on thermal conductivity, we examine existing approaches and their appropriateness to our investigation. Finally, the end of the report discusses the need for better mobility predictions in regions where seasonality is important and highly organic soils are prevalent. As part of this, we note omissions and shortfalls in current methods and outline how best to correct these using a combination of theory, laboratory work, and field tests.
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Preface

This study was conducted for the Assistant Secretary of the Army for Acquisition, Logistics, and Technology under project number 465395, “Boreal Aspects of Ensured Maneuver (BAEM),” which is part of the U.S. Army Engineer Research and Development Center (ERDC) 6.2 Remote Assessment of Infrastructure for Ensured Maneuver (RAFTER) Program managed by Ms. Danielle Whitlow, ERDC Geotechnical and Structures Laboratory (GSL). Dr. Sally Shoop was the technical monitor. This work is continuing under project number 471941, “Remote Assessment of Snow Mechanical Properties” and “Mobility in Peat and Northern Soils,” under the Entry and Sustainment in Complex Contested Environments Program managed by Dr. John Rushing, GSL.

The work was performed by the Terrestrial and Cryospheric Sciences Branch (CEERD-RRG) and the Force Projection and Sustainment Branch (CEERD-RRH) of the Research and Engineering Division (CEERD-RR), ERDC Cold Regions and Research and Engineering Laboratory (CRREL). At the time of publication, Dr. John Weatherly was Chief, CEERD-RRG; Dr. Harley Cudney was Acting Chief, CEERD-RRH; Mr. Jared Oren was Acting Chief, CEERD-RR; and Dr. Mark L. Moran was the Technical Director for military programs, CEERD-RZT. The Deputy Director of ERDC-CRREL was Mr. David B. Ringelberg, and the Director was Dr. Joseph L. Corriveau.

COL Ivan P. Beckman was Commander of ERDC, and Dr. David W. Pittman was the Director.
## Acronyms and Abbreviations

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Description</th>
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<tbody>
<tr>
<td>CEATS</td>
<td>Camp Ethan Allen Training Site</td>
</tr>
<tr>
<td>CRREL</td>
<td>U.S. Army Cold Regions Research and Engineering Laboratory</td>
</tr>
<tr>
<td>EAFR</td>
<td>Ethan Allen Firing Range</td>
</tr>
<tr>
<td>ERDC</td>
<td>Engineer Research and Development Center</td>
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<tr>
<td>FASST</td>
<td>Fast All-season Soil STrength</td>
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<td>FY</td>
<td>Fiscal Year</td>
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<tr>
<td>GSL</td>
<td>Geotechnical and Structures Laboratory</td>
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<tr>
<td>MEF</td>
<td>Marcell Experimental Forest</td>
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<tr>
<td>NATO</td>
<td>North Atlantic Treaty Organization</td>
</tr>
<tr>
<td>NRMM</td>
<td>NATO Reference Mobility Model</td>
</tr>
<tr>
<td>RAFTER</td>
<td>Remote Assessment of Infrastructure for Ensured Maneuver</td>
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<td>SPRUCE</td>
<td>Spruce and Peatland Responses Under Changing Environments</td>
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<tr>
<td>USCS</td>
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<tr>
<td>USDA</td>
<td>U.S. Department of Agriculture</td>
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1 Introduction

1.1 Background

The FY16 (fiscal year 2016) Baltic Maneuver study performed by the U.S. Army Engineer Research and Development Center’s Cold Regions Research and Engineering Laboratory (ERDC-CRREL) for the Night Vision and Electronic Sensor Directorate highlighted several critical gaps for maneuver capabilities against threats in northern climates. Among these are the inability to predict the strength of and mobility on highly organic soils and how these change seasonally. Terrain that is impassible in summer can become avenues of approach in winter.

Currently in NRMM (NATO [North Atlantic Treaty Organization] Reference Mobility Model), the frozen peat thickness needed to support a vehicle is determined using the method outlined by Shoop (1995). Shoop’s method is based on tabular values listed by Rummukainen (1984) and Hakkarainen (1949) of recommended frozen peat thicknesses needed to support different forms of transportation commonly used by Finish foresters. These “vehicles” range from a horse to a 10-ton truck. Their lists include values for both wet and dry soils and assume that the main failure mode of the frozen peat layer is by crushing. Shoop (1995) fit two curves (wet and dry) to these values to predict the minimum frozen peat thickness needed for a specific vehicle. Inputs are the vehicle weight and whether the soil is saturated or unsaturated. If the frost depth is greater than 50 cm, there is no deflection regardless of the surface loading. Shoop (1995) notes that the uniaxial compressive strength of frozen peat is similar to other frozen soils. For non-peat soils, regardless of organic content, NRMM assumes that a frozen layer thickness of 5 cm is capable of supporting a vehicle of any size (Richmond 1991). More recent efforts studying the impact of vehicle-induced stress and displacement on frozen silt, sand, and clay (Parker et al. 2009, Coutermash and Shoop 2009) have found that the current NRMM approach is too conservative.

According to Parker et al. (2009), moving vehicles can adequately be modeled as static loads. They also found that when investigating soil deflection due to applied loads, the soil could be modeled as a linear elastic material.
Saarilahti (1991) argued that plasticity theory should be used when modeling vehicle bearing capacity of soils. Suvinen (2002, 2006) also found that soil deflection was best described using plasticity theory and that frost effects on soil strength could easily be incorporated if the soil was assumed to be either cohesive or frictional but not a combination of both.

1.2 Objectives

The object of this study is to highlight current practices for estimating bearing capacities, thermal conductivity, and vehicle mobility on highly organic and peat soils and to show what could be done to better predict these values.

1.3 Approach

In this report, we begin by investigating the different methods for calculating the bearing capacity of frozen soils, including peat (section 2). First, we present the generalized plate theories, including failure criteria, for linear elastic, plastic, and modified plastic. In all instances, the plate is assumed to be uniform, circular, and of infinite extent.

In section 3, we propose a new method to calculate the thermal conductivity of highly organic soils based on de Vries’ (1963) and extended by Tian et al. (2016). In doing so, we first examine past approaches and compare them to our current method, which is based on Johansen (1975). Correctly quantifying how heat moves through the soil is not only important to being able to accurately predict the soil’s temperature but also to determining the ice and water contents, which are important to soil strength. Section 4 follows with a discussion of ice-affected material properties.

Finally, section 5 discusses current methods to forecast vehicle mobility on highly organic and peat soils. As part of this, we note omissions and shortfalls and how best to correct these.


2 Bearing Capacity of Frozen Peat

2.1 Linear elastic

Much work has been done on infinite elastic plates resting on a foundation (Timoshenko and Woinowsky-Kreiger 1959; Kerr 1996; Squire et al. 1996). The plate is assumed to be thin (20 < diameter; thickness < 100), homogeneous, circular, of uniform thickness, and of infinite extent. Another critical assumption is that the deflections are small (<<thickness). Figure 1 depicts the scenario.

Following Timoshenko and Woinowsky-Krieger (1959) the forces, \( P(r) \), on the plate are

\[
P(r) = q - R = D \frac{d^4 w}{dr^4},
\]

\[
D = \frac{Eh^3}{12(1-\nu^2)},
\]  

(1)
where

\[ q = \text{the applied load (Pa)}, \]
\[ R = \text{the reactive force of the foundation (Pa)}, \]
\[ w = \text{the displacement (m)}, \]
\[ D = \text{the flexural rigidity (bending stiffness) (N\cdot m)}, \]
\[ E = \text{Young's modulus (Pa)}, \]
\[ h = \text{the thickness (m)}, \] and
\[ \nu = \text{the Poisson ratio}. \]

An often-used simplification is that the foundation follows Winkler’s (1867) assumption that the reactive force is linearly proportional to the deflection. Thus,

\[ D \frac{d^4w}{dr^4} + \rho_f gw = q, \quad (2) \]

where

\[ \rho_f = \text{the foundation density (kg/m}^3\text{)} \] and
\[ g = \text{is the gravitational constant (m/s}^2\text{)}. \]

The solution to equation (2) is found in Wyman (1950) and reprinted in Squire et al. (1996). For a static point load at the center of the plate, the solution to equation (2) is

\[ w = -\frac{q}{2\pi \rho_f g \lambda^2} kei \left( \frac{r}{\lambda} \right) \quad (3) \]

\[ \lambda = (D/\rho_f g)^{1/4} \] is the characteristic length (m) and \( kei \) is a zero-order Kelvin function. The maximum deflection is located at the center of the plate and is

\[ w_{max} = \frac{q}{8\rho_f g \lambda^2} \quad (4) \]

since \( kei(r = 0) = -\pi/4 \) (Abramowitz and Stegun 1972).

For uniform circular loading, the solution to equation (2) is
\[
w = \begin{cases} 
\frac{P}{\rho_f g} \left[ 1 + \frac{a}{\lambda} \left( \text{ker}' \left( \frac{a}{\lambda} \right) \text{ber} \left( \frac{r}{\lambda} \right) - \text{kei}' \left( \frac{a}{\lambda} \right) \text{bei} \left( \frac{r}{\lambda} \right) \right) \right] & 0 \leq r \leq a \\
\frac{P a}{\rho_f g \lambda} \left( \text{ber}' \left( \frac{a}{\lambda} \right) \text{ker} \left( \frac{r}{\lambda} \right) - \text{bei}' \left( \frac{a}{\lambda} \right) \text{kei} \left( \frac{r}{\lambda} \right) \right) & r > a 
\end{cases}
\]

where \( a \) is the load radius and \( q = P/\pi a^2 \); \( \text{ker}, \text{ber}, \text{and bei} \) are zero-order Kelvin functions; and \(*'\) indicates the derivative with respect to \( r \). The maximum again occurs at the center of the plate and is given as (Wyman 1950)

\[
\omega_{\text{max}} = \frac{q}{\rho_f g} \left( 1 + \frac{a}{\lambda} \text{ker}' \left( \frac{a}{\lambda} \right) \right)
\]

since \( \text{ber}(r = 0) = 1 \) and \( \text{bei}(r = 0) = 0 \).

From Timoshenko and Woinowsky-Krieger (1959), the radial tensile strength \( (\sigma_r) \) and radial and angular bending moments \( (M_r, M_t) \) of a circular plate are

\[
\sigma_r = 6 \frac{M_r}{h^2} \\
M_r = -D \left( \frac{d^2 w}{dr^2} + \frac{\nu}{r} \frac{dw}{dr} \right) \\
M_t = -D \left( \nu \frac{d^2 w}{dr^2} + \frac{1}{r} \frac{dw}{dr} \right)
\]

The maximum bending moment occurs at the center of the plate where \( M_r = M_t \). Using equation (5) with \( z = r/\lambda \), we have (Abramowitz and Stegun 1972)
\[
\frac{dw}{dz} = \frac{Pa}{\rho_f g \lambda} \left( k e r' \left( \frac{a}{\lambda} \right) b e r'(z) - k e i' \left( \frac{a}{\lambda} \right) b e i'(z) \right)
\]
\[
= \frac{Pa}{\sqrt{2} \rho_f g \lambda} \left( k e r' \left( \frac{a}{\lambda} \right) \left( b e r_i(z) + b e i_i(z) \right) + k e i' \left( \frac{a}{\lambda} \right) \left( b e r_i(z) - b e i_i(z) \right) \right)
\]
\[
\frac{d^2w}{dz^2} = \frac{Pa}{\sqrt{2} \rho_f g \lambda} \left( k e r' \left( \frac{a}{\lambda} \right) \left( b e r_i(z) + b e i_i(z) \right) + k e i' \left( \frac{a}{\lambda} \right) \left( b e r_i(z) - b e i_i(z) \right) \right)
\]
\[
= \frac{Pa}{\rho_f g \lambda} \left( k e r' \left( \frac{a}{\lambda} \right) \left( -\frac{1}{z} b e r'(z) - b e i(z) \right) + k e i' \left( \frac{a}{\lambda} \right) \left( \frac{1}{z} b e i'(z) - b e r(z) \right) \right)
\]
so that

\[
M_r = -D \left( \frac{d^2w}{dr^2} + \frac{\nu dw}{r dr} \right) - D \left( \frac{d^2w}{dz^2} + \frac{\nu dw}{z dz} \right)
\]
\[
= -\frac{D}{\lambda^2} \left( P a \left( k e r' \left( \frac{a}{\lambda} \right) \left( -\frac{1}{z} b e r'(z) - b e i(z) \right) \right) \right)
\]
\[
+ \frac{\nu P a}{z \rho_f g \lambda} \left( k e r' \left( \frac{a}{\lambda} \right) \left( b e r'(z) - k e i' \left( \frac{a}{\lambda} \right) b e i'(z) \right) \right)
\]

The maximum stress occurs at the center of the plate where \( r = 0 \) (\( z = 0 \)).
Taking the limit of equation (9) using the polynomial expansions of the Kelvin functions and their derivatives (Abramowitz and Stegun 1972),

\[
(M_r)_{max} = \lim_{z \to 0} M_r = -\frac{P a D}{\rho_f g \lambda^3} \left( k e r' \left( \frac{a}{\lambda} \right) \left( 0 - 0 \right) + k e i' \left( \frac{a}{\lambda} \right) \left( \frac{1}{2} - 1 \right) \right)
\]
\[
\quad + \nu \left( k e r' \left( \frac{a}{\lambda} \right) (0) - k e i' \left( \frac{a}{\lambda} \right) \left( \frac{1}{2} \right) \right)
\]
\[
= \frac{P a D}{2 \rho_f g \lambda^3} (1 + \nu) k e i' \left( \frac{a}{\lambda} \right).
\]

Rearranging equations (7) and (10), assuming \( P_{cr} = \pi a^2 P \), it follows that the critical load, \( P_{cr} \), is
\[
P_{cr} = \frac{\pi a}{3(1+\nu)\lambda k\text{erf}\left(\frac{a}{\lambda}\right)} h^2 (\sigma_r)_{\text{max}}. \tag{11}
\]

Equation (11) is used to determine the load needed for first crack formation. This is not necessarily the same load required for ice failure, or breakthrough. Based on experimental data for both fresh and saline ice, it is assumed that \( \sigma_f > (\sigma_r)_{\text{max}} \) and \( P_f > P_{cr} \), where the subscript \( f \) indicates failure. Panfilov (1960) proposed an equation of the form

\[
P_f = \left(A_1 + B_1 \frac{a}{\lambda}\right) h^2 \sigma_f. \tag{12}
\]

This is the form used by Shoop (1995) and Richmond et al. (1995). Their work is based on guidelines used in Finland for forest operations on peat and bog lands (Rummukainen 1984). For frost depths \( h \) less than 0.5 m,

\[
P_f = \begin{cases} 
0.35h^2 & \text{for dry soil,} \\
0.86h^2 & \text{for wet soil,}
\end{cases} \tag{13}
\]

where the unit of \( P_f \) is meganewtons. Richmond et al. (1995) recommend that the dry soil version of equation (13) be used for all tracked vehicles and all wheeled vehicles weighing less than 12 tons. Also, even though equation (13) was developed for peat soils, it can be applied to other soils since the compressive strength of frozen peat is similar to other frozen mineral soils and falls within the range of frozen silts and clays (Shoop 1995).

### 2.2 Modified Plasticity Theory

#### 2.2.1 The Finnish Method

The Mohr-Coulomb theory states that (Suvinen 2002)

\[
\tau = c + q\tan\phi, \tag{14}
\]
where

\[ \tau = \text{shear strength (kN/m}^2) \],
\[ c = \text{soil cohesion (kN/m}^2) \],
\[ q = \text{the load (kPa)} \], and
\[ \phi = \text{the soil internal friction angle (°)}. \]

The general equation for “ultimate,” or critical bearing capacity \( P_f \) (kN), for a load at the surface is based on the work of Terzaghi (1943) and is presented by (Karafiath and Nowatzki 1978) as

\[
\frac{P_f}{\text{area}} = cN_c s_c i_c d_c + \gamma \frac{B}{2} N_\gamma s_\gamma i_\gamma d_\gamma,
\]  

(15)

where

\[ c = \text{soil cohesion (kN/m}^2) \],
\[ \gamma = \text{soil weight (kN/m}^3) \],
\[ s_c = \text{the shape factor for soil cohesion} \],
\[ s_\gamma = \text{the shape factor for soil weight} \],
\[ i_c = \text{the inclination factor for soil cohesion} \],
\[ i_\gamma = \text{the inclination factor for soil weight} \],
\[ d_c = \text{the depth factor for soil cohesion} \],
\[ d_\gamma = \text{the depth factor for soil weight} \],
\[ B = \text{the load width (m)} \],
\[ N_c = \text{bearing capacity factors for soil cohesion}, \text{ and} \]
\[ N_\gamma = \text{bearing capacity factors for soil weight}. \]

\( N_c \) and \( N_\gamma \) depend on only the soil friction angle. The ground and the vehicle load are assumed to be flat so that \( i_c = i_\gamma = 1 \). For purely cohesive soils, \( \phi = 0 \), and for purely frictional soils, \( c = 0 \).

For a rectangular footing, the Terzaghi shape factors are dependent on \( B/L \) where \( L \) (m) is the load length such that equation (15) for a shallow load becomes

\[
\frac{P_f}{LB} = \left[ 1 + 0.3 \left( \frac{B}{L} \right) \right] cN_c + \left[ 1 - 0.2 \left( \frac{B}{L} \right) \right] \gamma \frac{B}{2} N_\gamma. 
\]  

(16)
For a circular load, Terzaghi found that $s_c = 1.3$ and $s_\gamma = 0.6$ so that equation (15) simplifies to

$$\frac{P_f}{\pi r^2} = 1.3cN_e + 0.6\gamma \frac{2r}{2} N_\gamma$$

$$= 1.3cN_e + 0.6\gamma r N_\gamma,$$

where $r$ (m) is the load radius. For vehicles, this is the equivalent radius of the tire contact area. If the ground is frozen, Suvinen (2006) proposes that equation (17) becomes

$$\frac{P_f}{\pi r^2} = \left(1.3cN_e + 0.6\gamma r N_\gamma\right) \frac{B^*L^*}{BL},$$

$$B^* = B + 2h \tan \beta,$$

$$L^* = L + 2h \tan \beta,$$

where $\beta$ (°) is the pressure spreading angle in the soil and $h$ (m) is the frost depth. For vehicles, $B$ (m) and $L$ (m) are the width and length of the tire-soil contact area, respectively. Note that the frozen ground correction factor $(B^*L^*/BL)$ can also be applied to equation (16). In peats, $\tan \beta = 0.9$ while for mineral soils $\tan \beta = 1.0$.

Suvinen (2002) and Suvinen et al. (2003) argue that soils can be categorized as either purely cohesive ($\phi = 0^\circ$) or purely frictional ($c = 0$). Based on that, for cohesive soils he follows the work of Skempton (1951) who quantified the ultimate load for saturated clays as

$$\frac{P_f}{\text{area}} = cN_e$$

$$N_e = \begin{cases} 
6(1.2)\left(1 + 0.2 \frac{D_f}{B}\right) & \text{circle} \\
5\left(1 + 0.2 \frac{B}{L}\right)\left(1 + 0.2 \frac{D_f}{B}\right) & \text{rectangle}
\end{cases}$$

where $D_f$ (m) is the depth of the footing from the surface. Even though Suvinen uses the circular shape factors in equation (17), he uses the rectangular form of $N_e$ in equation (19). To account for freezing, Suvinen (2002,
2006) reinterprets Skempton’s (1951) formulation for the cohesion factor, \( N_c \), and critical load for cohesive soils as

\[
N_c = 5 \left( 1 + 0.2 \frac{B^*}{L} \right) \left( 1 + 0.2 \frac{h}{B^*} \right),
\]

(20)

\[
\left( \frac{P_f}{c} \right) = \pi r^2 (1.3cN_c) \frac{B^*L^*}{BL},
\]

where \( D_f \) in equation (19) is treated as the frost depth \( (h) \). Suvinen’s equation for the ultimate load for cohesive soils appears to include the shape factors twice since Skempton’s (1951) quantification of \( N_c \) already includes the effect of shape. Also, there should be consistency in using either the circular or rectangular forms. Thus, for circular loads, the correct form should be

\[
\left( \frac{P_f}{c} \right) = \pi r^2 c \left( 6(1.2) \left( 1 + 0.2 \frac{h}{B^*} \right) \right) \frac{B^*L^*}{BL}.
\]

(21)

For totally frictional soils, Suvinen (2002) follows the work of Balla (1962) so that

\[
N_\gamma = 0.0488\phi^3 - 3.6055\phi^2 + 90.9482\phi - 760.7648,
\]

(22)

\[
\left( \frac{P_f}{\gamma} \right) = \pi r^2 (0.6\gamma rN_\gamma) \frac{B^*L^*}{BL}.
\]

Note that equation (22) is only valid for \( 20^\circ \leq \phi \leq 40^\circ \). This is not a restriction for most natural soils but could affect results for compacted terrain and highly organic ones.

For wheeled vehicles, the equivalent tire radius is (Suvinen 2002, 2006)

\[
\text{contact area} = (\text{width})^{0.8} (\text{diameter})^{0.8} (\text{deflection})^{0.4},
\]

\[
L = \frac{\text{contact area}}{\text{width}},
\]

(23)

\[
r = \sqrt{\frac{\text{contact area}}{\pi}}.
\]
The tire deflection is the difference between the loaded and unloaded wheel radii (Suvinen 2002, 2006). The above equations assume that the tire contact width is the same as the actual tire width. For tracked vehicles, the equivalent radius is calculated using (Engineering ToolBox 2003)

\[ r = \frac{1.3 (BL)^{0.625}}{2 (B + L)^{0.25}}. \]  

(24)

2.2.2 Modifications to the Finnish approach

The approach outlined in the previous section assumed that the soils can be classified as either granular or cohesive, allowing for simplified quantification of the bearing capacity. Very few soils, however, are either purely granular or cohesive, especially during freezing. Thus, we argue that a more general quantification of the cohesion and weight-bearing capacity factors \( N_c \) and \( N_\gamma \), respectively, is needed. The method we used is that of Vesić (1973) based on the findings of Hjiaj et al. (2004). The factors are

\[
N_q = \exp(\pi \tan \phi) \tan^2 \left(\frac{\pi}{4} + \frac{\phi}{2}\right), \\
N_c = (N_q - 1) \cot \phi, \\
N_\gamma = 2(N_q + 1) \tan \phi.
\]

If the friction angle is zero, then \( N_c = 5.14 \) and \( N_\gamma = 0.0 \). Note that, for clayey soils, it is common practice (Fredlund and Rahardjo 1993) to calculate the stress using undrained conditions such that, \( N_c = 5.14 \).

The shape factors for rectangular loads are now

\[
s_c = 1 + \frac{N_q B}{N_c L}, \\
s_\gamma = 1 - 0.4 \frac{B}{L},
\]

(26)

and the corresponding depth factors are
For circular footings, $B/L = 1.0$. Following Suvinen's (2002, 2006) approach, the final equation for the ultimate load under freezing conditions becomes

$$\frac{P_f}{\text{area}} = \begin{cases} 
    c \left( 1 + \frac{N_q}{N_c} \frac{B^*}{L^*} \right) \left( 1 + 0.4 \frac{h}{B^*} \right) \left( N_q - 1 \right) \cot \phi & \frac{B^* L^*}{BL} \leq \frac{h}{B} \leq 1 \\
    + \gamma B \left( 1 - 0.4 \frac{B^*}{L^*} \right) (N_q + 1) \tan \phi & \frac{B^* L^*}{BL} > 1
    
\end{cases}$$

(28)

As can be seen from equation (28), the strength of soil is dependent not only on its physical properties but also on predicting the temperature, water content, and ice content. The ability to move heat, or energy, through a medium depends on the thermal conductivity and heat capacity. Section 3 will discuss the best approach to model the thermal conductivity of soil, including those with high organic content. Section 4 follows with how the soil physical properties change seasonally.
3 Thermal Conductivity of Organic Soils

Many researchers have studied the thermal conductivity of soil. Farouki (1981) summarized various methods for calculating the thermal conductivity ($\kappa$) of soils, including frozen ones. All methods can be quantified as experimental, semiempirical, or empirical. Representative examples of each include Kersten (1949), de Vries (1963), and Johansen (1975), respectively.

Kersten (1949) conducted thermal conductivity measurements in the laboratory on many different Alaskan soils, including peat. As well as looking at the effects of soil mineralogy, he also investigated soil wetness and freezing. From these, he developed semiempirical equations for coarse and fine-grain soils to predict the thermal conductivity as a function of density and water content for frozen and unfrozen states. His findings, as well as the approach of de Vries (1963) discussed further below, figured heavily in Johansen’s approach (1975).

3.1.1 Semiempirical methods

3.1.1.1 de Vries (1963)

de Vries' (1963) approach assumes that the soil behaves as a Maxwell-Fricke-type medium, that the particles are ellipsoidal, and that the soil sample is continuous (air or water) such that the thermal conductivity, $\kappa$, is

$$\kappa = \frac{\kappa_o f_o + \sum_{i=1}^{N} \kappa_i f_i \lambda_i}{f_o + \sum_{i=1}^{N} f_i \lambda_i},$$

(29)

where

- $o = \text{the soil medium, either water or air;}$
- $N = \text{the number of particle types (sand, clay, granite, silica, etc.);}$
- $f_i = \text{the volume fraction (m}^3/\text{m}^3\text{) of each component; and}$
- $\lambda_i = \text{is a component-specific weighting, or form, factor defined as}$
\[
\lambda_i = \frac{1}{3} \sum_{a,b,c} \left[ 1 + \frac{\kappa_i}{\kappa_o - 1} g_a \right]^{-1}
\]  

(30)

and \( g_a(a) + g_a(b) + g_a(c) = 1 \), where \( g_a(a,b,c) \) are shape factors. de Vries (1963) found good agreement with experiments if \( g_a(a) = g_a(b) = 0.125 \) and \( g_a(c) = 0.75 \). He also found that, for dry soils, equation (29) needed to be multiplied by 1.25. Farouki (1981) realized that equation (29) could be applied to moist or unsaturated soil if the water content was above a given minimum. Farouki (1981) found that de Vries’ (1963) approach could also be used for frozen soils. His version of equation (29) is

\[
\kappa = \frac{\kappa_w \theta_w + \kappa_i \theta_i + \left( \kappa_{air} + \kappa_{vapor} \right) f_{air} \lambda_{air} + \kappa_{soil} f_{soil} \lambda_{soil}}{\theta_w + \theta_i \lambda_{ice} + f_{air} \lambda_{air} + f_{soil} \lambda_{soil}}
\]

(31)

where \( \theta_w \) and \( \theta_i \) are the volumetric water and ice content \((m^3/m^3)\), respectively. The weighting factors, equation (30), are unchanged. Farouki also used the same shape factors for both the soil and ice. The new terms needed to describe unsaturated soils are

\[
\kappa_{vapor} = \kappa_{vapor}^{sat}
\]

\[
g_{a(air)} = 0.333 - \left( 0.333 - 0.035 \right) \frac{f_{air}}{n}
\]

\[
\theta_w \leq n
\]

(32)

where the constants in equation (32) are those for quartz sand and \( n \) is the soil porosity.

3.1.1.2 Tian et al. (2016)

Tian et al. (2016) introduced a simplified approach to de Vries (1963) and Farouki (1981) for frozen and unfrozen soils. They assume that vapor movement is negligible and thus \( \kappa_{vapor} = 0 \). Further, water is the continuous medium except when \( \theta_w = 0 \) such that
where $\kappa_{dry}$ is the dry thermal conductivity. Following Johansen (1975) and others, Tian et al. (2016) assumed that $\kappa_{sand} = \kappa_{quartz} = 7.7 \text{ W/m·K}$, $\kappa_{clay} = 1.93 \text{ W/m·K}$, $g_{a(sand)} = g_{a(quartz)} = 0.182$, and $g_{a(clay)} = 0.00775$. The thermal conductivity and shape factors for silt are used as fitting parameters. Although Tian et al.’s (2016) approach includes freezing soils, it does not consider organics. To validate their method, Tian et al. (2016) measured the thermal conductivity of 27 different unfrozen soils and 18 frozen samples by using the heat-pulse method and values reported in the literature.

### 3.1.2 Empirical methods

#### 3.1.2.1 Johansen (1975)

Johansen’s method (1975) has been widely used to quantify the thermal conductivity of soils, including peat, for both frozen and unfrozen soil. As part of his thesis work investigating existing mathematical models and published experimental results, he developed an empirical method. The dependent soil properties are porosity ($n$), dry density ($\rho_d$), volumetric unfrozen water content ($\theta_w$), volumetric ice content ($\theta_i$), quartz content ($f_{quartz}$), and organic fraction ($\theta_of$). Based on these, the thermal conductivity, $\kappa$ (W/m·K), is

$$
\kappa = \kappa_{dry} + \left(\kappa_{sat} - \kappa_{dry}\right) K_e, 
$$

(34)
where

\[
\kappa_{\text{dry}} = \frac{135\rho_d + 64.7}{2700 - 947\rho_d} \pm 20\%,
\]

\[\kappa_{\text{sat}} = \begin{cases} \kappa_w^n \kappa_{\text{soil}}^{(1-n)} & T > 273.15 K \\ \kappa_w^{(n-\theta_w)} \kappa_i^{(1-n)} & T \leq 273.15 K \end{cases},
\]

\[K_e = \begin{cases} \exp \left( 0.7 \log \frac{\theta_w}{n} + 1 \right) & T > 273.15 K \text{ coarse} \\ \exp \left( \log \frac{\theta_w}{n} + 1 \right) & T > 273.15 K \text{ fine} \\ \frac{\theta_w}{n} & T \leq 273.15 K \end{cases},
\]

\[\kappa_{\text{soil}} = \begin{cases} \kappa_{\text{quartz}}^{1-f_{\text{quartz}}-\theta_w} \kappa_{of}^{\theta_w} & f_{\text{quartz}} < 0.2 \\ \kappa_{\text{quartz}}^{2.0(1-f_{\text{quartz}}-\theta_w)} \kappa_{of}^{\theta_w} & \end{cases},
\]

\(\kappa_{\text{sat}}\) is the saturated thermal conductivity, and \(K_e\) is the Kersten number, or normalized thermal conductivity. The form of the dry thermal conductivity is based on de Vries’ (1963). The form of the Kersten number is based on the results of Kersten’s (1949) experiments. Farouki (1981) found that Johansen’s method for predicting soil thermal conductivity matched the existing data well except for the case of dry (\(\theta_w/n < 0.2\)), unfrozen, coarse soils.

3.1.2.2 Lu et al. (2007)

Lu et al. (2007) expanded on the Johansen (1975) and Côté and Konrad (2005) approaches. Specifically, they changed the form of the dependence of the Kersten number on the saturation ratio (\(S_r = \theta_w/n\)) to better represent measured values, especially for drier soils. Lu et al. (2007) also derived a new relation for the dry thermal conductivity for mineral soils. For \(K_e\), they proposed

\[K_e = \exp \left\{ \alpha \left[ 1 - S_r^{(\alpha-\beta)} \right] \right\},
\]

\[\alpha = \begin{cases} 1 & f_{\text{quartz}} < 0.2 \\ 0.2 & \end{cases},
\]

\[\beta = \begin{cases} 0 & f_{\text{quartz}} < 0.2 \\ 0.2 & \end{cases}.
\]
where $\alpha$ depends on soil texture and the shape parameter $\beta$ is 1.33 (Lu et al. 2007). Their new $\kappa_{\text{dry}}$ is

$$\kappa_{\text{dry}} = -an + b,$$

(40)

where $a$ and $b$ are empirical parameters. Based on experiments performed on eight different soil types, Lu et al. (2007) found that, for coarse soils (sand fraction > 40%), $\alpha = 0.96$; for fine grained soils, $\alpha = 0.27$; and for $0.2 < n < 0.5$, $a = 0.56$ and $b = 0.51.$

### 3.1.3 Current approach

Both the Noah (Niu et al. 2011) and FASST (Fast All-season Soil STrength) (Frankenstein and Koenig 2004) land surface models use a modified version of Johansen’s (1975) method to calculate the soil thermal conductivity to determine soil state, and hence soil strength, needed by NRMM. After a literature search, we chose the following thermal conductivity values (W/m·K) for the individual components in FAAST:

- $\kappa_{\text{quartz}} = 8.4$
- $\kappa_{\text{vapour}} = 0.025$
- $\kappa_{\text{air}} = 0.025$
- $\kappa_{\text{water}} = 0.57$
- $\kappa_{\text{ice}} = 2.2$
- $\kappa_{\text{organic}} = 0.25$
- $\kappa_{\text{non-quartz}} = 5.0$

$$\kappa_{\text{soil}} = \frac{1}{2} \kappa_{\text{organic}} \kappa_{\text{quartz}} \kappa_{\text{non-quartz}} (1 - f_{\text{quartz}} - f_{\text{organic}})$$

Following Peters-Lidard et al. (1998), FASST assumes that the quartz content is equal to the sand fraction. For peat soils, the coarse-grained soil quantification in equation (37) is used. For sands and gravels, the method of Lu et al. (2006), equation (39), is used but with the texture and shape parameters ($\alpha$ and $\beta$, respectively) of Tarnawski et al. (2009) (coarse: $\alpha = 0.728$, $\beta = 1.165$; fine: $\alpha = 0.37$, $\beta = 1.29$).
3.1.4 New approach

We consider two approaches to predict the thermal conductivity of peat and other highly organic soils. Both begin with the method of Tian et al. (2016). For the first, a separate term for organics is added to the numerator and denominator in the top of equation (33) while for the second the soil thermal conductivity and shape factors are modified to include the organic soils, such as for the Johansen (1975) method. These two approaches are

\[
K = \frac{K_w \theta_w + K_i \theta_i \lambda_i + K_{\text{air}} f_{\text{air}} \lambda_{\text{air}} + K_{\text{soil}} f_{\text{soil}} \lambda_{\text{soil}} + K_{\text{of}} \theta_{\text{of}} \lambda_{\text{of}}}{\theta_w + \theta_i \lambda_i + f_{\text{air}} \lambda_{\text{air}} + f_{\text{soil}} \lambda_{\text{soil}} + \theta_{\text{of}} \lambda_{\text{of}}},
\]

\[
K_{\text{soil}} = K_{\text{sand}} f_{\text{sand}} K_{\text{silt}} f_{\text{silt}} K_{\text{clay}} f_{\text{clay}},
\]

\[
g_{a(\text{soil})} = g_{a(\text{sand})} f_{\text{sand}} + g_{a(\text{silt})} f_{\text{silt}} + g_{a(\text{clay})} f_{\text{clay}},
\]

and

\[
K = \frac{K_w \theta_w + K_i \theta_i \lambda_i + K_{\text{air}} f_{\text{air}} \lambda_{\text{air}} + K_{\text{soil}} f_{\text{soil}} \lambda_{\text{soil}}}{\theta_w + \theta_i \lambda_i + f_{\text{air}} \lambda_{\text{air}} + f_{\text{soil}} \lambda_{\text{soil}}},
\]

\[
K_{\text{soil}} = K_{\text{sand}} f_{\text{sand}} K_{\text{silt}} f_{\text{silt}} K_{\text{clay}} f_{\text{clay}} \theta_{\text{of}},
\]

\[
g_{a(\text{soil})} = g_{a(\text{sand})} f_{\text{sand}} + g_{a(\text{silt})} f_{\text{silt}} + g_{a(\text{clay})} f_{\text{clay}} + g_{a(\text{of})} \theta_{\text{of}}.
\]

Tian et al. (2016) suggest that \( g_{a(\text{of})} = 0.5 \).

Table 1 gives volume fractions and other soil physical properties currently used by FASST for the 15 USCS (Unified Soil Classification Scheme) soil types (Frankenstein and Koenig 2004).

Typically, the organic fraction is given as a function of weight instead of volume by comparing the sample weight before and after burning off of the vegetable matter. Schaefer and Jafarov (2016) assume that the mass of carbon is 50% of the mass of organics in instances where the carbon content is known. The volume fraction of organics is \( \theta_{\text{of}} = M_{\text{of}} / \Delta z \rho_{\text{of}} \), where \( M_{\text{of}} \) is the mass of the organic matter, \( \Delta z \) is the layer thickness, and \( \rho_{\text{of}} \) is the layer density.
Table 1. Soil default physical properties.

<table>
<thead>
<tr>
<th>Soil Type</th>
<th>Bulk Dry Density $\rho_d$ (g/cm$^3$)</th>
<th>Porosity $n$</th>
<th>Quartz Content $q$</th>
<th>Organic Fraction $\theta_{of}$</th>
<th>Percent Sand $f_{sand}$ (%)</th>
<th>Percent Silt $f_{silt}$ (%)</th>
<th>Percent Clay $f_{clay}$ (%)</th>
<th>Percent Gravel $f_{gravel}$ (%)</th>
<th>Fine or Coarse</th>
</tr>
</thead>
<tbody>
<tr>
<td>GW</td>
<td>1.947$^2$</td>
<td>0.293$^2$</td>
<td>0.65</td>
<td>0.00</td>
<td>5</td>
<td>2</td>
<td>2</td>
<td>91</td>
<td>Coarse</td>
</tr>
<tr>
<td>GP</td>
<td>2.079$^{1,2}$</td>
<td>0.228$^{1,2}$</td>
<td>0.65</td>
<td>0.00</td>
<td>5</td>
<td>2</td>
<td>2</td>
<td>91</td>
<td>Coarse</td>
</tr>
<tr>
<td>GM</td>
<td>1.903$^2$</td>
<td>0.305$^2$</td>
<td>0.65</td>
<td>0.05</td>
<td>10</td>
<td>12</td>
<td>5</td>
<td>68</td>
<td>Coarse</td>
</tr>
<tr>
<td>GC</td>
<td>2.133$^1$</td>
<td>0.198$^1$</td>
<td>0.65</td>
<td>0.05</td>
<td>10</td>
<td>9</td>
<td>31</td>
<td>45</td>
<td>Coarse</td>
</tr>
<tr>
<td>SW</td>
<td>1.657</td>
<td>0.375$^{3,4}$</td>
<td>0.80</td>
<td>0.00</td>
<td>92$^6$</td>
<td>2$^6$</td>
<td>2$^6$</td>
<td>4</td>
<td>Coarse</td>
</tr>
<tr>
<td>SP</td>
<td>1.643</td>
<td>0.375$^{3,4}$</td>
<td>0.80</td>
<td>0.00</td>
<td>92$^6$</td>
<td>2$^6$</td>
<td>2$^6$</td>
<td>4</td>
<td>Coarse</td>
</tr>
<tr>
<td>SM</td>
<td>1.640</td>
<td>0.385$^{3,4}$</td>
<td>0.80</td>
<td>0.05</td>
<td>73$^{6,4}$</td>
<td>15$^{6,4}$</td>
<td>7$^{6,4}$</td>
<td>0</td>
<td>Coarse</td>
</tr>
<tr>
<td>SC</td>
<td>1.626</td>
<td>0.385$^{3,4}$</td>
<td>0.80</td>
<td>0.05</td>
<td>5</td>
<td>9</td>
<td>31$^{6,4}$</td>
<td>0</td>
<td>Coarse</td>
</tr>
<tr>
<td>ML</td>
<td>1.458</td>
<td>0.453$^{3,4}$</td>
<td>0.35</td>
<td>0.10</td>
<td>5</td>
<td>61</td>
<td>24$^{6,4}$</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>CL</td>
<td>1.528</td>
<td>0.430$^{3,4}$</td>
<td>0.05</td>
<td>0.10</td>
<td>5</td>
<td>27</td>
<td>58</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>OL</td>
<td>1.480</td>
<td>0.407$^{3,4}$</td>
<td>0.20</td>
<td>0.35</td>
<td>5</td>
<td>46$^{6,4}$</td>
<td>14$^{6,4}$</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>CH</td>
<td>1.445</td>
<td>0.468$^{3,4}$</td>
<td>0.05</td>
<td>0.10</td>
<td>5</td>
<td>28</td>
<td>57</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>MH</td>
<td>1.529</td>
<td>0.464$^{3,4}$</td>
<td>0.35</td>
<td>0.10</td>
<td>5</td>
<td>61</td>
<td>24</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>OH</td>
<td>1.568</td>
<td>0.437$^{3,4}$</td>
<td>0.20</td>
<td>0.25</td>
<td>5</td>
<td>16</td>
<td>54</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>PT</td>
<td>0.150</td>
<td>0.822$^5$</td>
<td>0.05</td>
<td>0.95</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>0</td>
<td>Fine</td>
</tr>
<tr>
<td>SMSC (MC)$^*$</td>
<td>1.658</td>
<td>0.384$^{3,4}$</td>
<td>0.80</td>
<td>0.05</td>
<td>65$^{6,4}$</td>
<td>18$^{6,4}$</td>
<td>12$^{6,4}$</td>
<td>0</td>
<td>Coarse</td>
</tr>
<tr>
<td>CLML (CM)$^*$</td>
<td>1.551</td>
<td>0.416$^{3,4}$</td>
<td>0.20</td>
<td>0.10</td>
<td>5</td>
<td>41</td>
<td>41</td>
<td>0</td>
<td>Fine</td>
</tr>
</tbody>
</table>

1 Seman and Shoop (2007)
2 Guymon et al. (1993), Table A1
3 USDA (2018)
4 Rollings and Rollings (1996), Table 2.11
5 Schwärzel et al. (2006), Table 3
6 Miller and White (1998)
7 Tarnawski et al. (1997), pp. 96
* The two letter designation is input into the model but is not the official USCS designation.

3.1.5 Unfrozen liquid water content

The liquid water content in frozen soils is dependent on how strong the bond is between the soil particles and the water and how cold the medium is. Schaefer and Jafarov (2016) give the volumetric liquid water content under freezing conditions as a fraction of the unfrozen water content, $\theta_w$: 

* The two letter designation is input into the model but is not the official USCS designation.
\[
(\theta_w)_i = \left( \frac{T_{\text{ref}} - T}{T^\ast} \right)^{b_i}
\]

\[
\theta_w = (1 - \theta_{of}) \left( f_{\text{sand}}(\theta_w)_{\text{sand}} + f_{\text{silt}}(\theta_w)_{\text{silt}} + f_{\text{clay}}(\theta_w)_{\text{clay}} \right) + \theta_{of}(\theta_w)_{of}
\]

For pure sand, silt, clay, and organics, the reference temperature \( T_{\text{ref}} \) is 0.1°C; the temperature offset, \( T^\ast \), is 0.01°C; and the empirical constant, \( b_i \), is \(-0.9\), \(-0.5\), \(-0.3\), and \(-1.0\), respectively.
4 Material Properties Parameterization

As discussed in section 2, soil physical properties vary depending on water, ice content, and temperature. In this section, we present how these parameters change seasonally and due to wetting and drying events.

4.1 Shear stress

Mohr-Coulomb’s law, equation (14), has been modified by researchers to account for both freezing and the degree of soil saturation. Matsushi and Matsukura (2006) included the effects of varying water content on shear strength for a sand and silt soil as

\[ \tau = C e^{-\alpha \theta_w} + \sigma' \tan \phi' , \]  

where

\[ \sigma' = \sigma - \mu = \text{the net normal stress}, \]
\[ \mu = \text{the pore water pressure}, \]
\[ \theta_w = \text{the volumetric water content}, \]
\[ \phi' = \text{the effective angle of shearing resistance}, \]
\[ C = \text{the maximum cohesion}, \]  
\[ \alpha = \text{related to the susceptibility of strength reduction}. \]

Of greater interest for this study is the effect of pore ice on shear strength. Ladanyi (2003) states that the behavior of sand and ice mixtures depends on the concentration of soil solids, \( C_s = 1 - n \), where \( n \) is the porosity. If \( C_s \leq 0.4 \) (\( n \geq 0.6 \)), pore ice governs behavior, while for \( 0.4 < C_s < 0.6 \), frictional resistance between particles dominates. Finally, for \( C_s \geq 0.6 \) (\( n \leq 0.4 \)), dilatancy between interlocking soil grains dictates the soil strength. Thus, assuming that the strain rate is equal to the critical one \((10^{-5} \text{ h}^{-1}, 2.78 \times 10^{-9} \text{ s}^{-1})\),
\[ \tau = \begin{cases} c(t,T) & C_s \leq 0.4 \ (n \geq 0.6) \\ \frac{c(t,T)}{2\sqrt{N_\sigma}} + \sigma \tan \phi & C_s > 0.4 \ (n < 0.6) \end{cases} \] (45)

\[ c(t,T) = \sigma_0 \left(1 + \frac{|T|}{1°C}\right)^w, \]

where \( T \) is temperature (°C) and \( c(t,T) \) is the temperature-affected cohesion. At a strain rate of \( 10^{-5} \text{ h}^{-1} \) and polycrystalline ice, \( \sigma_0 = 103 \text{ kPa} \) and \( w = 0.37 \).

### 4.2 Friction angle

The friction angle also changes depending on the water and ice contents. Dong et al. (2013) found that the friction angle decreased as the volumetric water content increased and fit an exponential curve to their data. As an aside, they found that roots had no effect. Yavari et al. (2016) found no relation between friction angle and temperature for temperatures above freezing for a clay and sand. They found that their results were similar to other published studies.

Arenson and Springman (2005) found for granular soils that the dependence of the friction angle on ice is

\[ \phi = 32.5 \left(1 - \theta_i^{2.6}\right), \] (46)

where 32.5 is the unfrozen friction angle and \( \theta_i \) is the volumetric ice content (0–1). Because the friction angle changes depending on the soil type, we propose a modification to equation (46):

\[ \phi = \phi_u \left(1 - \theta_i^{2.6}\right), \] (47)

where \( \phi_u \) is the unfrozen friction angle for which default values are listed in Table 2. This is used to calculate the plastic weight-bearing factors \( N_\gamma \), \( N_\alpha \), and \( N_q \) from equation (25).
Table 2. Soil parameters. Items in *pink* are considered to be cohesive in the dry state. All are for the unfrozen state.

<table>
<thead>
<tr>
<th>Soil</th>
<th>friction angle average</th>
<th>friction angle compacted</th>
<th>density (g/cm³)</th>
<th>porosity</th>
<th>Cohesion (kPa)</th>
<th>Cohesion compacted (kPa)</th>
<th>Young's Modulus (MPa)</th>
<th>Young's Modulus compacted (MPa)</th>
<th>Poisson ratio</th>
<th>Maximum Soil Strength, RCI (psi)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GW</td>
<td>36.5</td>
<td>50</td>
<td>1.947</td>
<td>0.293</td>
<td>0</td>
<td>70</td>
<td>107</td>
<td>0.25</td>
<td>300</td>
<td></td>
</tr>
<tr>
<td>GP</td>
<td>38</td>
<td>50</td>
<td>2.079</td>
<td>0.228</td>
<td>0</td>
<td>70</td>
<td>107</td>
<td>0.25</td>
<td>300</td>
<td></td>
</tr>
<tr>
<td>GM</td>
<td>35</td>
<td>35</td>
<td>1.903</td>
<td>0.305</td>
<td>5</td>
<td>74</td>
<td>81.5</td>
<td>0.25</td>
<td>750</td>
<td></td>
</tr>
<tr>
<td>GC</td>
<td>31.5</td>
<td>31.5</td>
<td>2.133</td>
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1 Average = 0.5*(min + max) as obtained from Geotechdata.info (2013).
3 Geotechdata.info (2014)
4 Onasch (2010)
4.3 Cohesion

Dong et al. (2013) found for low water contents that the soil cohesion increased linearly with water content but then decreased linearly after a certain point. Not enough soil types were tested to generalize the critical water content at which the transition occurs. Yavari et al. (2016) found that there was a nonlinear relation between cohesion and temperature for a clay for temperatures above freezing. Care should be taken in analyzing these results as they tested at only 5°C, 20°C, and 40°C.

4.4 Density

To compare the different approaches, the frozen states of certain physical properties are needed. Table 2 lists the unfrozen properties of 17 USCS soil types. The soil density for the frozen state is calculated as

$$\rho_{\text{tot}} = \rho_d + \rho_i n \theta_i,$$

(48)

where

- $\rho_d = \text{the dry density (g/cm}^3\text{),}$
- $n = \text{porosity, and}$
- $\rho_i = \text{ice density (0.92 g/cm}^3\text{).}$

For compacted, on-road scenarios, we assume that the dry density increases by 10%.

4.5 Young’s modulus

The frozen Young’s modulus (MPa) is (Lee et al. 2002)

$$E_f = -178 + 451 \rho_{\text{tot}}.$$

(49)

Care needs to be taken, though, when applying equation (49) to quantify the frozen Young’s modulus when the soil density is lower than 0.4 g/cm³. For most soils this is no problem, but it can be for highly organic soil.

Aukenthaler et al. (2016) assume a relation of the form

$$E_f = E_{f,\text{ref}} - E_{f,\text{inc}} \left( T - T_{\text{ref}} \right)$$

(50)
where \( E_{f,\text{ref}} \) is the frozen Young’s modulus at a reference temperature, \( T_{\text{ref}} \), and \( E_{f,\text{inc}} \) is the incremental change in \( E_f \) with temperature. What is unknown is whether equation (49) can be used to calculate \( E_{f,\text{ref}} \).

4.6 **Poisson ratio**

The Poisson ratio is the ratio of transverse strain to axial strain or how much “thinner” something becomes when pulled from the ends. For unfrozen soils, Li and Zhao (2014) found that the Poisson ratio increased with increasing temperature. Aukenetal. et al. (2016) found a similar relation for frozen sand, silt, and clay soils in situations where there was still liquid water present in the soil matrix. When the water is totally frozen, the soil becomes rigid.

4.7 **Effective soil strength**

The maximum soil strength \( (\sigma_r)_{\text{max}} \) (kPa) is needed for the elastic plate bending method, shown in equation (11). It is calculated as

\[
(\sigma_r)_{\text{max}} = c_i(\sigma_s)_{\text{max}} + \sigma_i n \theta, \tag{51}
\]

where \( (\sigma_s)_{\text{max}} \) is the maximum soil strength listed in Table 2 and \( c_i \) is a conversion factor. Since the ice strength, \( \sigma_i \), varies with temperature, impurities and age, among other things, we use three representative values: 103 kPa (Ladanyi 2003), 600 kPa (Fransson 2009), and 2500 kPa (Freitag and McFadden 1997) where the lower values are used for warmer temperatures.
5 Future Studies

The previous sections have pointed out the complexity of quantifying seasonal soil strength. Some work has been done on predicting soil strength of peat soils, but the approach is inconsistent. Most of the investigations on soil physical parameters have been carried out on pure soils and do not include the effect of organics. No unifying theory exists that combines seasonal changes in inherent soil properties with soil bearing capacity, especially at the scales needed to predict vehicle mobility.

Peat and highly organic terrain, as well as gravelly soils, cover large portions of Scandinavia, the Baltic States, and the Korean peninsula; and recently, interest in these areas has increased. The current military vehicle fleet has great difficulty traversing these terrain types except under certain conditions. Therefore, there is a great need to better understand vehicle and terrain interactions in these regions to better predict vehicle mobility. Determining seasonal impacts is crucial for these areas as terrain that is impassible during warmer months can become drivable when the temperature is below freezing.

Previous studies by Wong et al. (1979, 1982) focus on unfrozen peat and muskeg for a single condition, which does not look at the effect of changing moisture conditions or the effect of freezing or thawing. Other studies conducted on multiple peat and muskeg types (Radford and Rush 1961) report general observations but do not make any correlations between vehicle mobility and peat and muskeg type. Shoop (1995) and Richmond et al. (1995) developed equation (13) to represent the breakthrough limits for a frozen peat layer over a soft substrate. It does not provide sinkage or tractive force values needed to predict vehicle mobility on this soil type.

Unlike peat and muskegs, no similar studies have been conducted on gravelly soils. In part, this is because the gravel pieces make it difficult to measure any strength-related parameters, especially in the field. Both bevemeters and traditional cone penetrometers require fairly homogeneous soils. As a result, NRMM assumes these soils to always be at maximum strength regardless of gravel or moisture content.

New experimental data sets are required to create more accurate vehicle mobility predictions across multiple seasons for highly organic and gravelly terrains. Experiments should focus on collecting vehicle mobility and
soils characterization data on both terrain types when the soil is frozen, thawed, wet, and dry to see how mobility is affected by each of these ground states. Experiments should be conducted using both tracked and wheeled vehicles if possible. Vehicle measurements should include drawbar pull, motion resistance, sinkage, wheel speed, vehicle speed, and other key parameters. These measurements should be correlated with vegetation (above and below ground) and soil temperature, moisture, density, shear strength, California bearing ratio, and other measurable parameters.

5.1 Test site selection

Three potential test sites were visited during FY18. These were Camp Ethan Allen Training Site (CEATS), Vermont; William H. Miner Agricultural Research Institute (Miner’s), New York; and Marcell Experimental Forest (MEF), Minnesota. Each of these areas contain different terrain, soil, and vegetation conditions and seasonal extremes similar to Scandinavia, the Baltics, and the Korean Peninsula. Importantly, potential test sites must be vehicle accessible, fairly flat, and contain similar soils and vegetation to our areas of interest. We decided for FY19 to focus the field studies on the organic soils and to perform laboratory tests to characterize the strength of gravelly soils.

5.1.1 Camp Ethan Allen Training Site

CEATS is an 11,000-acre reserve located in northern Vermont and is home to the Army Mountain Warfare School (Figure 2). Based on the U.S. Department of Agriculture (USDA) soil map and the CEATS map, we selected three locations for possible testing. The first location is an old airstrip on the southern border that is flat and level, receives little traffic from the National Guard, and is an extensive and easily accessible space for vehicle testing (Figure 3).

The second and third locations contain taller grasses and vegetation typically found in wetter areas. While appropriate terrain conditions, they each pose slightly more difficult mobility challenges as shown in Figure 4 and Figure 5.
Figure 2. Geographic location and Topographical map of CEATS.

Figure 3. Old airstrip soil and terrain.

Figure 4. Range 6-3 vegetation and terrain.

Figure 5. Range 60 terrain.
5.1.2 William H. Miner Agricultural Research Institute

Miner’s is a research institute located in northern New York. It contains tiled and untiled terrain, peat and highly organic soils, easily accessible terrain, and the ability to test with any vehicles necessary (Figure 6). Miner’s is located in close proximity to EAFR, allowing experimental testing to be combined between the two facilities. This will shorten test events and will allow researchers and vehicles to travel between sites with minimal logistics required for moving equipment and test vehicles.

![Figure 6. Miner's soil and terrain.](image)

5.1.3 Marcell Experimental Forest

MEF is located in northern Minnesota and falls under the jurisdiction of the USDA Forest Service, Northern Research Station. It is home to the Spruce and Peatland Responses Under Changing Environments (SPRUCE) experiment. This is a multi-organization, 10-year experiment to measure the effects of warming and increased CO₂ on the peatland ecosystem. It is funded primarily by the U.S. Department of Energy and currently hosts in excess of 50 experiments. This and other studies by the University of Minnesota and the Minnesota research council at MEF provide a wide variety of current and historical measurements of the environment and seasonal soil conditions that will supplement data collected by any vehicle experiments. These groups share a common interest with CRREL in that they are also interested in vehicle mobility on peatlands to identify when they will support logging operations without causing destruction of the environment.

There are several sites at MEF with peat bogs and fens that provide unique sites for vehicle mobility research. We visited several of these in June 2018. These sites include Jennies Bog, Junction Fen (Figure 7), S7, Bog Lake Fen (Figure 8), and other unnamed locations. Each of these sites requires that vehicle testing occur in the winter only when the ground is frozen. The ground is too wet any other time of year; and the vehicles will become mired, causing large soil disturbances and likely immobilizing the
test vehicles. Junction Fen and Bog Lake Fen are the only ones feasible for vehicle testing as the others are too heavily vegetated or are inaccessible without major tree clearing.

Figure 7. Left, Junction Fen, showing temperature probe (center) and snow course markers (posts); right, Junction Fen grasses, sphagnum moss, and sun dew.

Figure 8. Bog Lake Fen, showing sparse trees and instrumentation.

Junction Fen is the best location for conducting vehicle mobility research and currently has a snow course across the fen where depth and density are measured annually, on-site power, and a temperature probe down to 2 m with measurements since the 1980s. It has almost no trees but does have small hillocks 25–75 cm high. The low vegetation includes leather leaf, grasses, sphagnum moss, pitcher plants, and sun dew. The peat thickness near the middle of the fen is approximately 3 m and is sapric (muck, contains less than one-sixth fibers by volume).

5.2 Field testing

Testing is currently scheduled to be conducted at EAFR and Miner's during FY19 because of the close proximity to CRREL and currently established permissions to conduct vehicle testing. Testing at MEF requires additional environmental permissions that will be pursued in FY19 in anticipation of FY20 field testing. Vehicle mobility testing will be conducted with an instrumented wheeled vehicle and a lightweight tracked vehicle (if available).
6 Conclusions

In this report we began by discussing different methods for calculating the bearing capacity of soils, including highly organic and gravelly ones. This was followed by a treatise of how the physical properties needed to determine the strength of soil change with temperature, water, and ice content. Next, we investigated the different approaches used to predict heat flow through soils and how these needed to be modified for organic soils. Finally, we presented the groundwork undertaken thus far to develop field and laboratory testing plans with which to validate the new methodology presented in this document as it relates to seasonal cross-country vehicle mobility.
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Metsäntutkimuslaitoksen tiedonantoja 390.


“Estimation of the Unsaturated Hydraulic Conductivity of Peat Soils: Laboratory


### Physical Properties of Highly Organic Soils and Their Importance to Mobility Considerations

#### Abstract

In this report, we begin by investigating the different methods for calculating the seasonal bearing capacity of soils, including highly organic ones such as peat. First, we present the generalized plate theories, including failure criteria, for linear elastic, plastic, and modified plastic. In all instances, the plate is assumed to be uniform, circular, and of infinite extent. The physical properties that determine soil strength change with temperature, water content, and ice content. It is therefore important to accurately predict these. Therefore, we include a section on calculating the soil thermal conductivity, which determines the flow of heat. Following the discussion on thermal conductivity, we examine existing approaches and their appropriateness to our investigation. Finally, the end of the report discusses the need for better mobility predictions in regions where seasonality is important and highly organic soils are prevalent. As part of this, we note omissions and shortfalls in current methods and outline how best to correct these using a combination of theory, laboratory work, and field tests.