

# Applying Particle Tracking Model in the Coastal Modeling System

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**PURPOSE:** This Coastal and Hydraulics Engineering Technical Note (CHETN) describes procedures to set up a particle tracking simulation through coupling the Coastal Modeling System (CMS) and Particle Tracking Model (PTM) in the Surface-water Modeling System (SMS). The step-by-step CMS-PTM setup is illustrated by a coastal application at Noyo, CA.

**INTRODUCTION:** The CMS is an integrated wave, current, sediment transport, and morphology change model for coastal and inlet applications (Buttolph et al. 2006; Lin et al. 2008) that was developed by the Coastal Inlets Research Program (CIRP). The Particle Tracking Model (PTM) was developed jointly by CIRP and the Dredging Operations and Engineering Research (DOER) program as a tool to compute the fate and pathways of sediments and other waterborne particulates in coastal engineering and dredging operations (MacDonald et al. 2006; Demirbilek et al. 2008). CMS-PTM is implemented in the SMS (Aquaveo 2010), which is a graphical user interface utility for PCs developed by the U.S. Army Corps of Engineers (USACE).

**NOYO NEARSHORE SEDIMENT PLACEMENT PILOT STUDY:** Noyo Harbor and Noyo River are located on the northern California coast. Every year about 30,000-40,000 cy of beachquality sediment is dredged from the Noyo River Federal Navigation Channel. The USACE San Francisco District (SPN) and the Coastal and Hydraulics Laboratory (CHL), U.S. Army Engineer Research and Development Center, are presently collaborating with the Noyo Harbor District and stakeholders in a pilot study to investigate a potential candidate site for nearshore placement of dredged sediment. Upland disposal sites used in the past will soon be exceeded. The pilot study proposes a dispersive nearshore site 3 to 8 miles north of Noyo Bay along the northern California coast (Figure 1).

To evaluate the potential impacts of nearshore placement, a Short-Term Fate of Dredged Material Model (STFATE) and CMS were applied for the study. SPN has applied STFATE to calculate near-field sediment transport and suspended sediment concentration during the placement of the dredged material. The USACE CIRP applied the CMS and CMS-PTM to simulate sediment transport for combined waves and currents under various ambient conditions and project alternatives. The model results will provide the technical information necessary to evaluate a demonstration site that is economically feasible for the optimum sediment placement location.

**CMS-PTM:** The CMS calculates water levels, currents and waves through the coupling of a hydrodynamic model, CMS-Flow and a wave spectral model, CMS-Wave. CMS-Flow also simulates sediment and salinity transport, and morphology change.

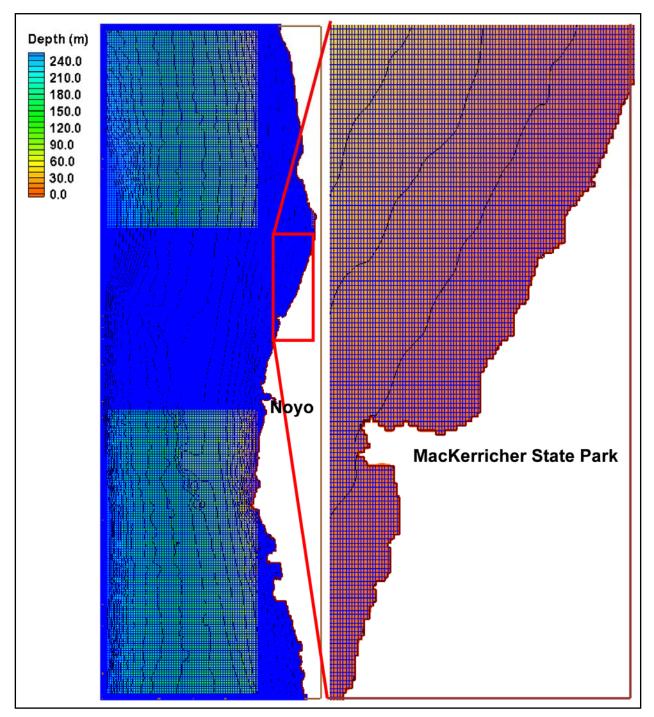


Figure 1. CMS domain, grid, and bathymetry.

CMS-Flow is driven by time-dependent water surface elevation at the offshore open boundaries, and wind forcing over the surface boundary. Directional wave data for input to CMS-Wave are available from the National Data Buoy Center (NDBC, *http://www.ndbc.noaa.gov*) and Coastal Data Information Program (CDIP, *http://cdip.ucsd.edu*). The wave conditions are specified at the seaward boundaries.

CMS-Flow requires three input files and CMS-Wave requires six input files through the SMS. Each of the CMS-Flow and CMS-Wave simulations will generate its own output file (Figure 2).

| Open                 |   |                 | ? 🔀    |
|----------------------|---|-----------------|--------|
| Look in:             | 🗀 Noyo  | • E 🕂 💷 •       |        |
| My Recent            | <pre> flow-exist-Alt2.cmcards flow-exist-Alt2_grid.h5 flow-exist-Alt2_mp.h5 </pre>          | CMS-Flow Input  |        |
| Documents            | flow-exist-Alt2_sol.h5 →<br>wave-exist-Alt2.dep   | CMS-Flow Output |        |
| Desktop              | wave-exist-Alt2.eng<br>wave-exist-Alt2.sim<br>wave-exist-Alt2.std<br>wave-exist-Alt2.struct | CMS-Wave Input  |        |
| My Documents         | I wave-exist-Alt2.txt J<br>wave-exist-Alt2.wav →  | CMS-Wave Output |        |
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Figure 2. CMS files.

The CMS-Flow input and output files are required, while the CMS-Wave output files are optional for setting up a CMS-PTM simulation. After loading the required hydrodynamic and/or wave files, users can follow the steps below to set up the CMS-PTM simulation for the Noyo application.

- **1. Native Sediment Dataset:** CMS-PTM requires spatially varying native bed sediment data specified as datasets, including the grain size information of d35, d50, and d90 for each cell, in the CMS-Flow grid.
  - i) Select and open the CMS-Flow control file, *"flow-exist-Alt2.cmcards"* (Figure 2).
  - ii) Choose *Data* | *Data Calculator* in the CMS-Flow menu.
  - iii) Name the first dataset, d35, in the *Output data set name* and specify a constant value, 0.1 mm in the *Calculator*.
  - iv) Click *Compute* to generate the dataset.
  - v) Repeat steps iii) and iv) to generate the datasets for d50 and d90 (Figure 3), (for the Noyo simulation, d50=0.2 mm and d90=0.4 mm).

| Ataset Toolbox<br>Tools<br>- Math<br>- Compare data sets<br>- Data Calculator<br>- Temporal<br>- Sample time steps<br>- Compute derivative<br>- Conversion<br>- Scalar to Vector<br>- Vector to Scalar<br>- Modification<br>- Map activity<br>- Filter | Data Calculator<br>Data Sets<br>Alt3 (CMS-Flow)<br>123 a. D50<br>123 b. Hard Bottom<br>123 c. ManningsN<br>2 d. Depth<br>3 imulation<br>123 e. Bathymetry<br>123 f. Capacity<br>123 g. Concentration<br>123 h. Current_Magnitude<br>123 j. Water_Elevation | Time Steps   |
|--|--|--|
|  | Add to Expression Data Set Info  | Calculator<br>( ) min<br>* In x^y max<br>- log sqrt ave<br>+ 1/x abs trunc |
| Update Available Tools<br>Help   | Output data set name: d35  | Compute  |

Figure 3. Generate the datasets, d35, d50, and d90.

- vi) Click Done to exit the Data Calculator.
- vii) Highlight the datasets, d35, d50, and d90, right-click, and select Export Datasets (Figure 4).
- viii) Select *XMDF file* in the *File Type*, check *All time-steps* in the *Time-steps*, and click the *Filename* to save the file "NativeSediments.h5" in the present working folder.
- 2. Land-water Interface Boundary Strings: CMS-PTM requires specifications of both open and closed boundaries. Open boundaries are specified in CMS-Flow, so closed boundaries need to be added for CMS-PTM (future versions of SMS will automatically generate the closed boundaries). The steps to perform this task are described as follows:
  - i) Choose *Cellstring* | *Generate Along Boundary* (this step will generate redundant boundary strings overlapped with existing strings along open boundaries) (Figure 5).
  - ii) Choose the *Select Cellstring* tool and select the *Land boundary* along the open boundary.
  - iii) Right-click and choose *Delete* (Figure 5).

| Export Data Set 🛛 🗙                                   | Save   |        | ? 🗙            |
|---|--|--------|----------------|
|   | Save in: 🔂 Noyo  | ▼      |                |
| File Type   | My Recent If flow-exist-Alt2_sol.h5  |        |                |
|   | Documents  |        |                |
| Time Steps<br>C Current time step<br>ⓒ All time steps | Desktop<br>My Documents  |        |                |
| Filename  | My Computer  |        |                |
| Help Save Cancel                                      | My Network File name: <u>NativeSediments.h5</u><br>Places Save as type: (*.h5) | •<br>• | Save<br>Cancel |

Figure 4. Generate the native sediment file.

- iv) Repeat steps ii) and iii) to delete other *Land boundary* cellstrings overlapped with existing open boundaries if more than one open boundaries exist in CMS-Flow.
- v) Save the project.
- **3. Sediment Sources:** Particles can be released from different source options. In CMS-PTM, sediment sources can be specified as points, lines, or areas. For the Noyo application, an area source was designated to represent the nearshore placement of dredged materials from a barge. The steps for creating the source file in SMS are:
  - i) Switch to the *Map Module* by clicking the icon  $\checkmark$ .
  - ii) Right-click the *default coverage* and choose *Type* | *Models* | *PTM* after generating the rectangular area for the sediment release (Figure 6).
  - iii) Choose the *Select Feature Polygon* icon 🔊 and click on the area source.
  - iv) Right-click the polygon, select *Attributes*, and the *Feature Object Attributes* will pop up.
  - v) Select the *Horizontal Polygon Source* in the *Type* (Figure 7).
  - vi) Specify *Date/Time* for the particle release, *Parcel Mass (kg)*, released mass *Rate (kg/m^2/s)*, and *Median Grain Size (mm)* of released particles (Figure 7).
  - vii) Save the area source specification as a map file.

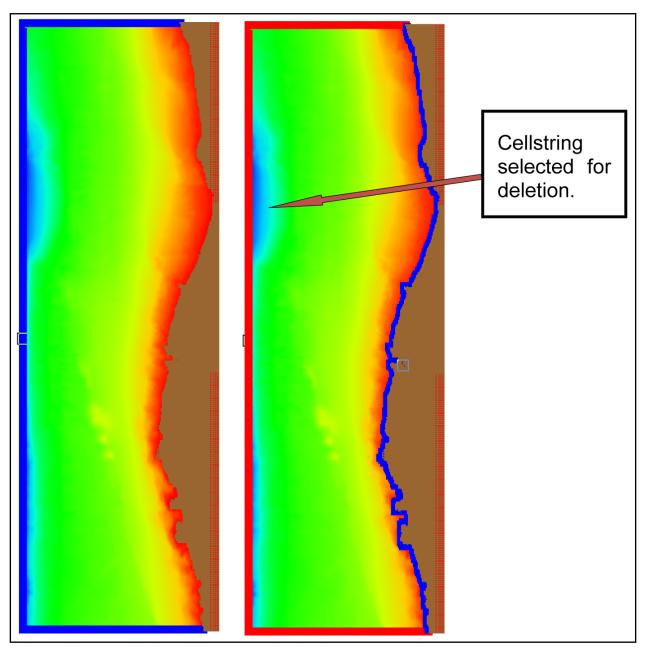


Figure 5. Generate the boundary cellstrings.

| 🖴 SMS 10.1 - [Part     | t.sms]   |                                      |    |   |    |     |     |       |
|------------------------|--|--------------------------------------|----|---|----|-----|-----|-------|
| 🔄 File Edit Display Fe | ature Objects Web                                      | o Window Help                        |    |   |    |     |     | _ 8 × |
| 🧉 🖬 🍜 🏦 🛛 😫            | 0.5 2  | ×                                    | Y. | Z | S: | Vx. | Vy: |       |
| PartSet                | Duplicate<br>Rename<br>Convert<br>Reprojet<br>Metadata | Cepth (m) 300.0 240.0 120.0 60.0 0.0 |    |   |    |     |     |       |
|                        | Type   | (1839386.0, 70                       |    |   |    |     |     |       |

Figure 6. Link source file to CMS-PTM.

| pe: Horizontal Polygon Sc | ource 🔽     | Source ID    | : 1       |                   |                    |              |               |                           |                           |
|---------------------------|-------------|--------------|-----------|-------------------|--------------------|--------------|---------------|---------------------------|---------------------------|
| ame: Default Polygon Name | •           |              |           |                   | 🗌 🗆 Show Co        | ordinates ir | n Spreadsheet |                           |                           |
| Date/Time                 | Parcel Mass | Vert. Radius | Rate      | Median Grain Size | Standard Deviation | Density      | Fall Velocity | Critical Shear Initiation | Critical Shear Deposition |
|                           | (kg)        | (m)          | (kg/m²/s) | (mm)              | (Phi-units)        | (kg/m²)      | (m/sec)       | (N/m²)                    | (N/m²)                    |
| 8/2/2008 8:00:00 AM 🛛 💌   | 10.0        | 1.0          | 0.0002    | 0.0257            | 0.8                | 2650.0       | -1.0          | -1.0                      | -1.0                      |
| 8/2/2008 8:10:00 AM 🛛 🔽   | 10.0        | 1.0          | 0.0002    | 0.0257            | 0.8                | 2650.0       | -1.0          | -1.0                      | -1.0                      |
| 8/2/2008 8:10:01 AM 🛛 🔽   | 10.0        | 1.0          | 0.0       | 0.0257            | 0.8                | 2650.0       | -1.0          | -1.0                      | -1.0                      |
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|                           | 110.0       | 10           | 0.0002    | 0.0257            | no                 | 2620.0       | 10            | 10                        | 10                        |

Figure 7. Define particle release scenario from the area source.

- **4. CMS-PTM Setup:** After the hydrodynamic data, native sediment data, source file, and boundary cellstrings are generated, users can follow the steps below to specify the CMS-PTM parameters and set up the CMS-PTM simulation.
  - i) Switch to *Particle Module* by clicking the icon **S**.

- ii) Choose *PTM* | *New Simulation*.
- iii) Choose *PTM* | *Model Control*.
- Simulation time (Figure 8).
  - i) Specify the starting time of the completed CMS-Flow simulation in the *Hydrodynamics*.
  - ii) Specify the starting and ending times of a CMS-PTM run in the *Simulation*.
  - iii) Specify the time-step for the CMS-PTM simulation and the output time interval in the *Particle Output*.
  - iv) Specify how often to update the sediment parameters and the hydrodynamic variables.

The starting time of CMS-Wave and the time-step for the wave forcing update need to be specified if waves are included in the simulation and selected in the *Files* page.

| PTM Model Control for Simula   | ation: PartSet   | $\mathbf{X}$  |
|--|--|---|
| Time Files Computations Output   |  |   |
|  | PTM Model Timing   |   |
| Simulation Run<br>Hydrodynamics<br>Sources<br>Waves  |  | 22 Fri 1 Mon  |
| Aug 2008   | Date/Time  |   |
| Simulation<br>Start: 8/ 2/2008 12:00:00 AM<br>Stop: 8/31/2008 12:00:00 AM                                  | Particle Output<br>Every: 36 time steps<br>(01:00:00.00 hh:mm:ss)  | Shears, Bedforms, and Mobility Update<br>Every: 36 time steps<br>(01:00:00.00 hh:mm:ss)                             |
| Ouration: 2505600.000 seconds     Time Step: 100.000 seconds   | Mapping Output<br>Every: 1000 time steps<br>(27:46:40.00 hh:mm:ss) | Flow and Elevation Update<br>Every: 36 time steps<br>(01:00:00.00 hh:mm:ss)   |
| Waves           Start:         8/ 2/2008 8:00:00 AM ▼           Time Step:         10800.0         seconds | Hydrodynamics<br>Start: 8/ 2/2008 12:00:00 AM 💌                    | Start:         8/ 2/2008 12:00:00 AM I           Stop:         1/ 2/1950 12:00:00 AM I           Last timestep trap |
| Help   |  | OKCancel  |

Figure 8. CMS-PTM model control pages (*Time*).

- Links to hydrodynamic and sediment data (Figure 9).
  - i) Click *Select paths* under the *XMDF Path* and set *Alt2/Datasets/Depth* for the *Depth Path*.
  - ii) Select the CMS solution file, *flow-exist-alt2\_sol.h5*, in the working folder for the *Hydrodynamics*.

| Description                    | Options                     |         | Filename         | XMDF Path |             |          |            |
|--------------------------------|-----------------------------|---------|------------------|-----------|-------------|----------|------------|
| Grid                           | CMS-Flow (XMDF)             | -       | PartAlt2_grid.h5 | Select p  | aths        |          |            |
| Hydrodynamics                  | CMS-Flow                    |         | Select file      | N/A       |             |          |            |
| Boundary conditions            | Existing file               |         | Part_Alt2_mp.h5  | N/A       |             |          |            |
| Sediment source                | Existing file               | -       | Select file      | N/A       | Select XMD  | F D-4h   |            |
| Neighbor                       | Create when model is run    | -       | Select filename  | N/A       | Select XMD  | r Paun   |            |
| Native sediments grain size    | XMDF data set               |         | Select file      | N/A       | Description | Options  | XMDF Path  |
| Тгар                           | Not included in simulation  | -       | N/A              | N/A       | Grid Path   | Required | Alt2       |
| Waves and breaking             | Not included in simulation  | -       | N/A              | N/A       | Depth Path  | Required | Alt2/Datas |
|                                | Not included in sinteletion |         |                  | 108       |             |          |            |
| Create input file(s) from data |                             |         |                  | 1025      |             |          |            |
| Create input file(s) from data |                             | Filenar |                  | 1028      |             |          |            |
| Create input file(s) from data |                             |         |                  |           |             | 10       | Canc       |

Figure 9. CMS-PTM model control pages (Files).

- iii) Set *Simulation/Current\_Velocity* for the *Velocity*, and *Simulation/Water\_Elevation* for the *Water surface elevation*.
- iv) Select *default coverage* in the *Sediment source* and name the *part.source* in *Select file-name*.
- v) Select *create when model is run* in the *Neighbor* and name the *part.neighbors* in *Select filename*.
- vi) Include *Waves and breaking* by selecting *CMS-Wave* and click *options* to obtain wave input for CMS-PTM (Figure 10).
- vii) Click the icon it to browse the working folder and to link the wave simulation file, *wave-exist-Alt2.sim*, under the *Parent Grid Geometry* | *CMS simulation file*.
- viii) Click the icon Load (\*.wav) to link the wave input file, *wave-exist-Alt2.wav*, under the *Parent Grid Solution Data*.
- *ix)* Specify the *Number of Spectra in file*.
- *x)* Click *OK* to complete the specifications of the page.

Because the wave simulation is included in CMS-PTM, it is necessary to return to the previous (*Time*) page to specify the *Start* time and the *Time-step* under the *Waves* (Figure 8).

| Waves  |   |
|--|---|
| - Parent Grid Geometry<br>CMS simulation file: 🔲 C:\Noyo\wave-exist-Alt2.sim | Nested Grid Geometry Use Nested Grids CMS simulation file: (none selected)  |
| Parent Grid Solution Data  | Note: The nested and parent grids must have the same number<br>of frames and the same times associated with each frame<br>Nested Grid Solution Data<br>Delete |
| Number of Spectra in file: 248   | ↓<br>Load (*.wav)<br>Number of Spectra in file must be the same as the Parent Grid<br>Delete  |
| Load (*.brk)   | Load (#.brk)  |

Figure 10. Specifications of wave input.

• Computation parameters and output

Most of the options in the *Computations* page are default for this Noyo application, except that the 3D mode is selected (Figure 11). In the *Output* page (Figure 12), *Print default keywords* is selected in the *File Output*, and *Source* and *State* are selected in the *Particle Output*.

**5. CMS-PTM Results:** As described in the previous sections for the Noyo application, CMS-PTM was designed to investigate the fate and transport of dredged materials under the combined influence of waves and currents from proposed placement sites.

The placement site, a rectangular area of  $86,600 \text{ yd}^2$ , is located about 4 miles north of Noyo Harbor near MacKerricher State Park. The CMS-PTM simulation is for August 1–30, 2008. In this application, clay materials were released at a level of 1 m above the ocean bottom at a rate of twice daily for 12 days. Each release lasted 10 minutes to mimic the barge placement operation. Figures 13 and 14 show the snapshot of calculated clay particle distributions at the end of the release (day 12) and the end of simulation (day 30), respectively. The simulation shows that clay particles either follow the waves propagating towards shore or move southward, driven by the northerly wind in this summer period. A good portion of the fine sediments can move past Noyo Bay to the model's south boundary and some out of the model domain through the simulation. At the end of the simulation, about 65 percent of the released clay particles are considered "dead,"

which means that they are either permanently buried at the sea bed or have moved out of the model domain.

| PTM Model Control for                            | Simulation: PartSet                       |                                   |
|--|---|-----------------------------------|
| Time Files Computations Outp                     | ut]                                       |                                   |
| Computation Methods                              | Computational Parameters                  |                                   |
| Advection: 3D 💌                                  | Bed porosity: 0.4                         | Temperature: 15.0 °C              |
| Centroid: Rouse                                  | Bed density: 2650.0 kg/m <sup>3</sup>     | Salinity: 34.0 ppt                |
| Distribution: By grain size 💌<br>Eulerian: PTM 💌 | Minimum depth: 0.01 m                     |                                   |
| Velocity: 2D (Logarithm                          | Diffusion Parameters Horizontal           | Vertical                          |
| Numerical scheme: 2                              | Min. diffusion coefficient: 0.0 m²/s      | 0.0 m²/s                          |
|  | Turbulent diffusion scalar: 0.25          | 0.00859                           |
|  | Wave diffusion scalar: 5.0                |                                   |
| Model Calculation Options                        |   |                                   |
| Currents   | ✓ Hiding and exposure                     | Residency (polygon trap required) |
|  | Particle-bed interaction                  | Wave mass transport               |
| Neutrally buoyant particles                      | ✓ Turbulent shear                         |                                   |
| Gedforms   | Source and trap Z-value relative to datum |                                   |
| Help   |   | OK Cancel                         |

Figure 11. Specifications of CMS-PTM parameters.

Figure 12. Selections of CMS-PTM output.

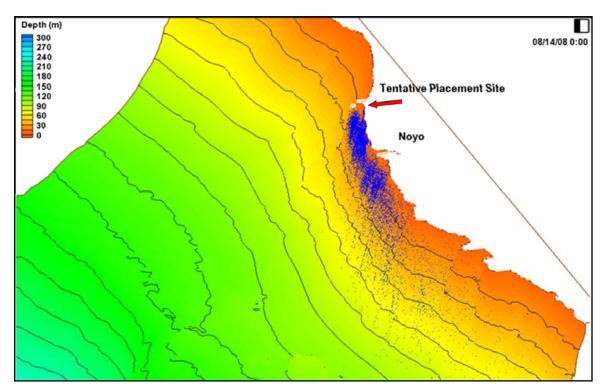


Figure 13. An oblique view of calculated clay particle distribution at the end of the release (day 12). The white square indicates the release area.

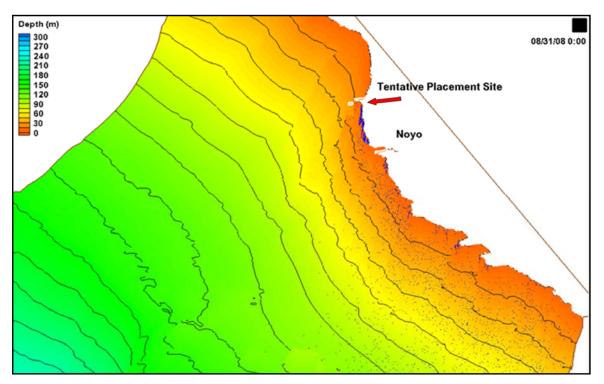


Figure 14. An oblique view of calculated clay particle distribution at the end of the simulation (day 30). The white square indicates the release area.

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