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Model tests in ice of a Canadian Coast Guard R-class icebreaker

Jean-Claude Tatinclaux

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report presents the results of resistance and propulsion tests in level ice of a 1:20-scale model of the R-class icebreaker of the Canadian Coast Guard. On the basis of the model test results, full-scale performance is predicted and compared with available full-scale trials data. Predicted ice resistance and required propeller rpm, thrust and delivered power are lower than full-scale measurements. This disagreement was attributed to the fact that the ship model had a much lower ice friction coefficient than the prototype. On the other		

20. Abstract (cont'd)

hand, predictions of thrust and power for a given ship speed and propeller rpm are in good agreement with corresponding full-scale measurements.

PREFACE

This report was prepared by Dr. Jean-Claude Tatinclaux, Research Hydraulic Engineer, of the Ice Engineering Research Branch, Experimental Engineering Division, U.S. Army Cold Regions Research and Engineering Laboratory. This study was CRREL's contribution to an international project proposed by the Committee on Ships in Ice Covered Waters at the 16th International Towing Tank Conference.

This report was technically reviewed by Dr. George D. Ashton (CRREL) and Dr. Hung T. Shen (Clarkson College, Potsdam, N.Y.).

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NOMENCLATURE

a, b, c	coefficients
B	ship beam
D	propeller diameter
E	ice elastic modulus
f	ice-hull friction coefficient
F_n	Froude number based on ice thickness
g	acceleration of gravity
h_i	ice thickness
h_s	snow cover thickness
J_v	apparent advance coefficient = $V/n_A D$
k	coefficient of proportionality between snow resistance and snow thickness
K_Q	torque coefficient = $Q/\rho_A n_A^2 D^5$
K_T	thrust coefficient = $T/\rho_A n_A^2 D^4$
ℓ	ice characteristic length
L_b	twice the bow length from stem to maximum beam (at water line)
n_A	average rate of propeller revolution
N	normal load on ice sample during friction tests
P_{DI}	delivered power in ice = $2\pi n_A Q_A$
Q_A	average propeller torque
r	correlation coefficient
R_i	net resistance in level ice
R_{is}	net resistance in pre-cut ice
R_{it}	total resistance in level ice
R_{ow}	resistance in ice-free water
R_s	resistance from snow cover
t	thrust deduction coefficient
T	draft; also tangential force on ice sample during friction test
T_A	propeller thrust
V	ship speed
β	stem angle with horizontal
δ	flare angle at maximum beam
θ	bow opening angle
ν	ice Poisson's ratio
λ	geometric model scale
ρ	water density
γ	water specific weight = ρg
σ	ice flexural strength

MODEL TESTS IN ICE OF A CANADIAN COAST GUARD R-CLASS ICEBREAKER

J.C. Tatinclaux

INTRODUCTION

The Committee on Ships in Ice-Covered Waters of the International Towing Tank Conference (ITTC), of which the U.S. Army Cold Regions Research and Engineering Laboratory (CRREL) is a member organization, developed a test program for an icebreaker model to be carried out by all organizations possessing ice model basins willing and able to participate in this international program. The test program was outlined in the Committee Report to the 16th ITTC (Committee on Ships in Ice-Covered Waters 1981). The test results obtained by the participating organizations were to be gathered and analyzed by Dr. R.V. Milano for presentation at the 17th ITTC in September 1984 in Goteborg, Sweden. The icebreaker model selected by the Committee was that of the most recent Canadian R-class icebreaker and was provided by the National Research Council of Canada (NRCC). Two model scales were chosen, namely 1:20 and 1:40. Resistance and propulsion tests were to be carried out with the 1:20-scale model in those ice test basins large enough to accommodate models of that size. Other tanks were to host only resistance tests on the 1:40-scale model since propulsion tests for such a small model would not produce meaningful results.

This report presents the results of the resistance and propulsion tests performed at CRREL with a 1:20-scale model.

SHIP CHARACTERISTICS

The Canadian Coast Guard is operating two R-class icebreakers, the CCGS Radisson and the CCGS Franklin. Model tests were made both in ice-free water (Murdey 1980) and in ice (Noble and Bulat 1979). Field trials were also carried out with both icebreakers (Edwards et al. 1981, Michailidis and Murdey 1981).

The R-class icebreaker is designed to break continuously through 1 m (3 ft) of level ice. The ship has a displacement of approximately 8000 tons at

FOREBODY

**TOWING
POST**

**VARIABLE
SPEED
MOTOR**

**RPM
COUNTER**

**TORQUE
AND THRUST
DYNAMOMETERS**

AFTBODY

Figure 1. Ship model.

Table 1. Principal particulars of hull and propellers.

	Full-scale	1:20-model
L _{WL}	93.00 m	4.65 m
L _{pp}	87.96 m	4.40 m
Draft T (level)	6.94 m	0.35 m
Max. waterline beam B	19.37 m	0.97 m
Displacement	7630 m ³	0.95 m ³
C _B	0.611	
C _{max}	0.918	
C _p	0.665	
C _w	0.799	
Number of propellers	2	
Prop. diameter D	4.12 m	0.206 m
Pitch/diameter	0.775	
Expanded area ratio	0.670	
Number of blades	4	
L _{WL} - length at water line		
L _{pp} - length between perpendiculars		
C _B - block coefficient		
C _{max} - maximum section coefficient		
C _p - prismatic coefficient		
C _w - waterplane area coefficient		

a midship draft of 6.9 m and is propelled by twin fixed-pitch propellers with a total shaft power of 11,000 kW.

The main hull and propeller characteristics of the ship are listed in Table 1 for both the full-scale size and the 1:20-scale model. Photographs of the model are shown in Figure 1.

HULL-ICE FRICTION COEFFICIENT

For determining the friction coefficient between ice and the ship model hull, NRCC had provided a flat board with the same surface finish as the hull.

A 20- by 20-cm ice sample cut from the ice sheet in the test basin was loaded with a total weight of 725 N (163 lb) and dragged over the board at a constant speed of 8 cm/s, approximately, by a linear actuator. The friction force was measured by a 44-N (10-lb) load cell connecting the actuator rod and the ice sample holder. The top and bottom surfaces of the ice were tested under both dry and wet conditions.

The results of the friction measurements are listed in Table 2. As can be seen from the data, the friction coefficient was practically independent of ice surface (top or bottom) and test conditions (dry or wet), with an overall average value of

$$f = 0.041 \pm 0.004.$$

It should be noted that this f -value for the model is extremely low because of the very smooth surfaces of the fiber glass ship's hull and test board. The full-scale ship is likely to have a higher friction factor. Edwards et al. (1981) gave friction factors of 0.30 at low speed and 0.19 at high speed. No values were reported by Michailidis and Murdey (1981).

Table 2. Results of friction tests.

Test conditions	Normal Force N (N)	Tangential Force T (N)	$f = T/N$	Average f
Ice top dry	725.00	30.51	0.042	0.041 ± 0.005
	725.00	24.60	0.034	
	725.00	29.71	0.041	
	725.00	27.85	0.038	
	725.00	33.94	0.047	
	725.00	32.34	0.045	
Ice bottom dry	725.00	28.20	0.039	0.044 ± 0.003
	725.00	30.34	0.042	
	725.00	32.92	0.045	
	725.00	32.92	0.045	
	725.00	33.98	0.047	
	725.00	31.94	0.044	
Ice top wet	725.00	27.49	0.038	0.043 ± 0.004
	725.00	29.22	0.040	
	725.00	34.30	0.047	
	725.00	34.07	0.047	
	725.00	31.72	0.044	
	725.00	30.56	0.042	
Ice bottom wet	725.00	24.55	0.034	0.038 ± 0.002
	725.00	27.05	0.037	
	725.00	27.13	0.037	
	725.00	28.07	0.039	
	725.00	28.11	0.039	
	725.00	29.85	0.041	

RESISTANCE TESTS

Resistance tests in ice-free water

For comparison with the open water resistance tests made at NRCC, as well as for aiding later analysis of the tests in level ice, a series of resistance tests were run in ice-free water over the range of velocities to be used in the ice tests.

The results of the open water resistance tests are listed in Table 3 and shown graphically in Figure 2, where both the CRREL data and NRCC data are presented. The NRCC data were calculated from the results presented by Murdey (1980), adjusted to a water temperature of 0°C. The CRREL data are, in the average, 20% larger than those measured at NRCC.

In the CRREL tests the ship model was equipped with the two propellers, while fairing cones were fitted to the bossings in the NRCC tests. In addition the tripwires used as turbulence stimulators in the NRCC resistance tests were not fitted to the model during the CRREL ice-free resistance tests since they would have severely interfered with the following resistance tests in ice. For those reasons the CRREL results were expected to be higher than those obtained at NRCC.

It should also be mentioned that the towing and load measurement apparatus of the CRREL test basin are designed for ice loads that are usually significantly higher than those measured in ice-free resistance tests, and that the accuracy of the measurements is on the order of ± 5 N.

For use in later analysis, the CRREL data were fitted by the following relationship

Table 3. Results of resistance tests in ice-free water.

V (m/s)	Resistance (N)*	
	CRREL	NRCC
0.68	4.89	7.22
0.77	11.03	8.82
0.88	14.37	11.30
1.01	14.59	14.42
1.05	18.82	15.59
1.14	15.57	18.27
1.26	31.36	22.33
1.30	33.23	23.56
1.36	34.96	25.51
1.38	36.83	26.58
1.49	39.72	32.13
1.61	54.00	38.20
1.73	60.10	47.20

*Resistance measured in CRREL ice basin and resistance measured at NRCC.

Figure 2. Model resistance in ice-free water.

$$R_{ow} = 18.73 V^{1.93} \quad (1)$$

in which R_{ow} (resistance in ice-free water) is expressed in N and V (ship speed) in m/s.

Resistance tests in level ice

The ITTC test program called for tests in full-scale ice thicknesses of 70 and 45 cm, corresponding to model ice thicknesses of 3.5 and 2.25 cm for the 1:20-scale model, and full-scale ice flexural strengths of 800 and 400 kPa, 40 and 20 kPa for the model. The ship velocities to be investigated were 0.5, 1.5 and 2.5 m/s at full scale (0.11, 0.34 and 0.56 m/s at model scale) for the stronger ice and 0.5, 2.5 and 5.5 m/s at full scale (0.11, 0.56 and 1.23 m/s at model scale) for the weaker ice.

The actual range of parameters tested were 2 to 4 cm for ice thickness, 25 to 50 kPa for ice flexural strength and 0.11 to 1.3 m/s for the velocity. The ice thickness was measured with a precision caliper. The ice flexural strength was obtained from in-situ tests of small cantilever beams. The beams were cut with a length of 7 to 10 times the ice thickness and a width 1.5 to 2 times the thickness. The load was applied downward at the tip of the beams by a hand-held Chatillon push-pull gauge. The elastic modulus E of the ice was measured by the plate deflection method.

A total of 20 tests were run; the test conditions and results are listed in Table 4. The net ice resistance R_i was calculated as the difference between the measured total resistance R_{it} and the ice-free resistance R_{ow} obtained from Figure 2. In ice resistance tests, the open water resistance is often considered negligible as compared to the ice resistance; however, in the present tests at the higher velocities (1 m/s or more, model scale), the open water resistance could be as high as 25-30% of the total resistance and could not be neglected.

Resistance tests in precut ice

In an attempt to differentiate among the various components of the level ice resistance of a given ship hull, tests were also run through precut ice. In the tests, a channel of width only slightly larger than the maximum beam of the model was hand sawed in the level ice sheet. The ice within this channel was cut into more or less regular pieces of average size similar to that which had been observed in the track left by the ship during the resistance tests through level ice. Six such tests were run for the range of ve-

Table 4. Results of resistance tests in level ice.

V (m/s)	h_i (cm)	σ (kPa)	E (MPa)	R_{it}^* (N)	$R_{ow}^\dagger$ (N)	R_i^{**} (N)
0.13	2.84	47.00	94.00	57.00	0.00	57.00
0.38	3.00	47.00	94.00	67.75	3.50	64.25
0.35	3.12	55.00	40.00	89.00	3.00	86.00
0.62	3.55	50.00	40.00	96.10	7.20	88.90
0.13	3.72	45.00	40.00	75.20	0.00	75.20
0.13	3.61	25.00	32.00	32.10	0.00	32.10
0.62	3.66	25.00	32.00	64.50	7.20	57.30
0.37	4.00	25.00	32.00	49.80	3.30	46.50
0.11	2.06	39.00	33.00	23.30	0.00	23.30
1.31	2.15	55.00	35.00	113.90	32.00	81.90
0.59	2.25	47.00	33.00	51.60	6.60	45.00
0.12	2.15	30.00	33.00	21.40	0.00	21.40
1.19	2.27	45.00	33.00	99.20	26.00	73.20
0.60	2.41	38.00	33.00	45.40	6.80	38.60
0.11	2.15	26.00	25.00	25.80	0.00	25.80
0.57	2.33	30.00	25.00	48.00	6.40	41.60
1.28	2.46	35.00	25.00	98.30	30.00	68.30
0.11	3.54	25.00	30.00	32.80	0.00	32.80
0.33	3.78	30.00	30.00	60.20	2.90	57.30
0.56	3.96	34.00	30.00	73.70	6.00	67.70

*Total measured resistance.

†Resistance in clear water, from CRREL tests.

** $R_{it} - R_{ow}$.

locity and ice thickness investigated in the level ice test. The corresponding data are listed in Table 5.

Analysis of resistance tests

In the tests through pre-cut ice, the ice resistance R_{is} should be a function of only the ice thickness h_i and ship speed V . Dimensional analysis indicates that the dimensionless resistance $R_{is}/\gamma B h_i^2$, with

γ = specific weight of water and B = ship beam, should be only a function of the Froude number $F_n = V/\sqrt{gh_i}$. Regression analysis of the data yielded

$$\frac{R_{is}}{\gamma B h_i^2} = 1.89 + 1.53 F_n^{1.27} \quad (2)$$

with a correlation coefficient $r = 0.987$.

Table 5. Results of resistance tests in pre-cut ice.

V (m/s)	h_i (cm)	R_{it}^* (N)	$R_{ow}^\dagger$ (N)	R_{is}^{**} (N)
0.11	2.38	12.46	0.00	12.46
0.56	2.26	26.70	6.00	20.70
1.24	2.51	67.17	27.00	40.17
0.11	3.75	26.69	0.00	26.69
0.35	4.10	44.48	3.20	41.28
0.57	4.26	52.53	6.30	46.23

*Total resistance in pre-cut ice.

†Resistance in clear water, from CRREL tests.

** $R_{it} - R_{ow}$.

The resistance through level ice, in its dimensionless form, was then assumed to differ from eq 2 by only a power function of the dimensionless ice strength $\sigma/\gamma h_i$. Nonlinear regression analysis of the data yielded

$$\frac{R_i}{\gamma B h_i^2} = 1.89 + 1.53 F_n^{1.27} + 8.2 \times 10^{-4} \left(\frac{\sigma}{\gamma h}\right)^{1.7} \quad (3)$$

with a correlation coefficient of 0.966.

The dimensional form of eq 3 for the 1:20-scale model is then

$$R_i = 1.796 h_i^2 + 6.328 V^{1.27} h_i^{1.37} + 0.040 h_i^{0.3} \sigma^{1.7} \quad (4)$$

in which R_i is expressed in N, h in cm, V in m/s and σ in kPa.

Other forms of the resistance equation

Several forms of the resistance in level ice have been proposed in the literature. The forms of these equations are usually based either on regression analysis of model tests or on physical consideration or on both. Among the equations proposed are those by Edwards (1980), eq 5a; Enkvist (1972), eq 5b; Poznyak and Ionov (1981), eq 5c; and Vance (1974), eq 5d,

$$R_i = a h_i^2 + b h_i V^2 + c h_i \sigma \quad (5a)$$

$$R_i = a h_i + b h_i V^2 + c h_i \sigma \quad (5b)$$

$$R_i = a h_i + b V^2 + c h_i \sigma \quad (5c)$$

$$R_i = a h_i^2 + b h_i^{0.65} V^2 + c h_i \sigma \quad (5d)$$

in which the coefficients a , b and c for a particular ship are to be determined from model tests. When the level ice resistance data obtained in the present model tests were analyzed according to the above formulas, the following values for the coefficients a , b and c and the corresponding correlation coefficients r were obtained

Formula	a	b	c	r
eq 5a	-0.082	10.08	0.404	0.976
eq 5b	-0.791	8.78	0.440	0.977
eq 5c	-0.125	19.46	0.434	0.971
eq 5d	0.238	11.93	0.403	0.975

for R_i in N, h_i in cm, V in m/s and σ in kPa. All of these various forms of the resistance equation lead to practically identical values of the correlation coefficient. However, except for Vance's form, they require a negative coefficient of the term in h_i or h_i^2 , usually referred to as the submergence component of the ice resistance, which is unrealistic.

Comparison with analytical predictors

Several empiric-analytical and purely analytical methods and equations for predicting ship resistance in level ice have been proposed. The earliest one is that by Kashtelyan et al. (1968) who expressed the ice resistance by

$$R_i = \mu_0 [0.004 B h_i \sigma + 3.6 B \gamma_i h_i^2] + \frac{2450}{\eta_2} B^{1.65} h_i V \quad (5e)$$

where R_i is expressed in N, B and h_i in m, σ in Pa and V in m/s, and γ_i is the specific weight of ice in N/m^3 . The coefficients μ_0 and η_2 are the so-called Shimansky coefficients, and are functions of the bow geometry. For the R-class icebreaker, $\mu_0 = 1.95$ and $\eta_2 = 1.50$. It should be noted that the numerical coefficients in eq 5e were determined from model tests and full-scale measurements on the Soviet icebreaker Ermak, and are valid for a velocity range of 0 to 2.8 m/s (5.5 knots), full-scale, and a maximum ice thickness of 1 to 1.2 m.

Purely analytical methods have been presented by Milano (1973), Naegle (1980) and more recently by Carter (1983). Milano's and Naegle's methods require extensive and sophisticated computer programs not available at CRREL and so could not be tested against the present model test results. Carter's approach, through a series of assumptions and simplifications, led to a relatively simple equation, which in a consistent system of units reads

$$R_i = \sigma h^2 \left[1 + 0.4 \frac{\rho V^2}{\sigma} \frac{\ell^2}{h_i^2} \right]^{1/2} (A_1 + A_2) \frac{B}{\ell} \quad (5f)$$

where ρ = density of water

ℓ = ice characteristic length,

$$\ell = \left[\frac{E h_i^3}{12 \gamma (1-\nu^2)} \right]^{1/4}$$

and A_1 and A_2 are parameters that characterize the ship hull

$$A_1 = 0.5483 \left(\frac{\pi}{2} - \theta \right) \frac{\sin \theta \sin \beta + f \cos \beta}{\sin \theta \cos \beta - f \sin \beta}$$

$$A_2 = 0.75 \frac{1 + 2 \cos \beta}{(\sin \theta + \cos \theta) (1 + 2 \sin \delta)} \left\{ \tan \beta + f \left(\frac{L_b}{B} \frac{2}{1 + 2 \cos \beta} + 1.732 \tan \beta \right) \right\}$$

where $L_b/2$ $\equiv$ bow length from stem to maximum beam

β $\equiv$ stem angle with the horizontal

δ $\equiv$ flare angle at maximum beam

θ $\equiv$ bow opening angle.

Figure 3. Comparison between ice resistance measurements and predictions by Kashtelyan's (Kashtelyan et al. 1968) and Carter's (1983) equations.

Figure 4. Comparison between ice resistance measurements and predictions by Carter's (1983) equation with $E/\sigma=5000$.

The measured resistance of the R-class model is compared in Figure 3 against the resistance predicted by eq 5e and 5f. All predictions are larger than the measured resistance, in particular those by Kashtelyan's equation (eq 5e) for the tests in thicker and weaker ice. It should be noted that the ice-hull friction coefficient does not appear explicitly in eq 5e, but is implicitly contained in its empirical coefficients. It should also be noted that actual icebreakers usually have a higher friction factor (on the order of 0.15 to 0.25) than that of 0.04 measured with the tested model, which is likely to account for some of the difference between Kashtelyan's predictions and the measured values of the model ice resistance.

Linear regression analysis between Carter's prediction and test results yielded

$$R_i - \text{measured} = 0.73 (R_i - \text{Carter})$$

with a correlation coefficient $r = 0.945$. Carter's derivation of eq 5f suffers from serious weaknesses in the physical description of the ice-breaking phenomenon, and it would have been dismissed if comparison between predicted values and full-scale and model measurements of ice resistance for a number of ships had not shown extremely good agreement. However, in comparing his predictions with available data, Carter always assumed a ratio E/σ of 5000. When applying eq 5f to the present test conditions, with the condition $E = 5000 \sigma$, there was remarkable agreement between predictions and measurements as shown in Figure 4. Linear regression analysis of the data in Figure 4 yielded

$$R_i - \text{measured} = 0.915 (R_i - \text{Carter}, E/\sigma = 5000)$$

with a correlation factor $r = 0.945$.

PROPULSION TESTS

In the model propulsion tests, each propeller shaft is connected to a thrust and torque dynamometer. The input shafts of the dynamometer are driven by a 746 W (1-hp) variable speed motor through T-joints and a 1:1.7 gear reducer as shown in the photographs of Figure 1.

In these tests, the model remains connected to the towing post of the test basin carriage. The carriage speed V and propellers' rpm are set to preselected values, and the thrust and torque on the propellers are measured together with the pull exerted on the towing post.

Prior to the propulsion tests per se, bollard tests (i.e., tests at $V = 0$ for a range of propeller rpm) were run for two reasons: to check the overall propulsion assembly by comparing the measured pull against that measured in the NRCC facilities (Murdey 1980), and to calibrate the dynamometers against the NRCC results since CRREL does not have the equipment necessary to perform in situ calibration of the dynamometers.

Bollard tests

The results of the forward bollard tests are listed in Table 6. The pull is the actual force measured at the towpost force block, the thrust and torque listed are the sum of the thrust and torque for both propellers calibrated against the NRCC data. The pull measured in these bollard tests is compared to that obtained at NRCC (Murdey 1980) in Figure 5, which shows that the two sets of data are in perfect agreement.

Figure 5. Comparison of pull force measured in forward bollard tests at CRREL and NRCC.

Table 6. Results of forward bollard tests (thrust and torque are total measured values for both propellers).

Rpm	Pull (N)	Thrust (N)	Torque (Nm)
224.00	14.37	15.97	0.40
281.00	23.98	25.58	0.63
282.00	23.35	24.95	0.61
333.00	33.81	35.85	0.87
336.00	34.83	35.67	0.91
338.00	34.38	36.56	0.92
338.00	35.41	35.85	0.92
390.00	47.20	51.07	1.20
390.00	46.71	50.80	1.24
390.00	47.60	48.75	1.22
442.00	61.39	64.37	1.57
442.00	61.16	63.34	1.56
448.00	63.03	65.97	1.64
500.00	79.13	83.49	2.00
501.00	79.71	84.52	2.03
503.00	80.51	84.87	2.04
550.00	97.15	103.02	2.45
551.00	98.17	101.55	2.48
553.00	96.75	102.31	2.50
553.00	98.80	101.42	2.49
608.00	120.10	123.57	3.02
610.00	120.90	125.75	3.05
612.00	119.17	124.73	3.12
612.00	122.28	126.11	3.07
659.00	142.08	143.81	3.56
661.00	141.81	148.93	3.72
671.00	148.39	152.57	3.72
714.00	167.74	169.48	4.19
720.00	164.72	173.75	4.35
765.00	193.19	195.99	4.81
822.00	225.12	233.58	5.60
425.00	58.91	61.15	1.51
447.00	65.40	68.00	1.68
470.00	72.20	75.20	1.85
514.00	86.90	90.60	2.22
537.00	94.70	98.80	2.42
559.00	102.60	107.20	2.63
581.00	111.00	116.20	2.84
626.00	128.80	135.00	3.29
648.00	138.30	145.00	3.53
671.00	148.10	155.30	3.78
693.00	158.40	166.00	4.04
716.00	169.40	177.00	4.30
738.00	180.70	188.40	4.57

Propulsion tests

Twenty-four tests were run to cover the range of velocity, ice thickness and ice strength required in the test program of the ITTC committee. The test conditions and tests results are listed in Table 7.

To check the proper functioning of the thrust and torque dynamometers and, if necessary, to adjust or correct the thrust and torque measurements, forward bollard tests in ice-free water were conducted immediately before and after each propulsion test.

From the results obtained for each pair of tests run at nominally identical velocity, ice thickness and ice strength, but at two different propeller speeds, the propellers' rpm at which the pull would be zero (self-propulsion point) was interpolated as well as the corresponding propeller thrust and torque. The corresponding total resistance of the model in ice-covered water was calculated as $R_{it} = R_i + R_{ow}$ with R_i given by eq 2 and R_{ow} by eq 1. The results are given in Table 8. In both Tables 7 and 8, the thrust T_A and torque Q_A are the total values for both propellers.

Table 7. Results of propulsion tests in level ice (thrust and torque are total measured values for both propellers).

V (m/s)	h_i (cm)	σ (kPa)	E (MPa)	n_A (rpm)	Pull (N)	T_A (N)	Q_A (Nm)
0.11	2.74	37.00	48.00	236.00	-18.00	23.60	0.40
0.11	2.71	30.00	48.00	334.00	8.80	40.70	0.88
0.56	2.61	43.00	48.00	358.00	-36.60	30.30	0.92
0.56	2.66	40.00	48.00	490.00	-0.90	77.90	1.69
1.19	2.68	50.00	48.00	510.00	-84.40	72.80	1.95
1.27	2.79	45.00	48.00	694.00	-14.30	121.00	3.10
0.11	2.69	26.00	13.00	222.00	-17.50	15.20	0.35
0.11	2.75	22.00	13.00	332.00	11.10	31.10	0.83
0.55	2.80	27.00	13.00	332.00	-35.10	40.10	0.73
0.52	2.90	25.00	13.00	497.00	9.70	71.90	1.90
1.26	2.80	28.00	13.00	443.00	-100.90	38.50	1.04
1.26	2.85	28.00	13.00	670.00	-29.40	111.10	2.84
0.11	3.70	24.00	12.00	269.00	-21.20	20.40	0.54
0.11	3.70	18.00	12.00	368.00	8.20	41.80	1.03
0.33	3.65	25.00	12.00	377.00	-48.20	39.10	1.14
0.29	3.70	25.00	12.00	520.00	14.80	80.10	2.02
0.53	3.85	30.00	12.00	399.00	-54.00	40.70	1.34
0.58	3.90	30.00	12.00	608.00	25.80	111.10	2.66
0.11	3.20	38.00	41.00	337.00	-12.30	35.90	0.87
0.11	3.30	35.00	41.00	502.00	41.90	80.10	1.99
0.34	3.40	43.00	41.00	393.00	-32.90	47.90	1.33
0.34	3.47	41.00	41.00	612.00	41.80	115.00	2.97
0.55	3.52	44.00	41.00	446.00	-53.70	54.30	2.12
0.55	3.70	44.00	41.00	720.00	48.80	162.90	4.12

Table 8. Calculated self-propulsion points of model.

V (m/s)	h_i (cm)	σ (kPa)	R_{it} (N)	n_A (rpm)	T_A (N)	Q_A (Nm)	J_V	K_T	$10 K_Q$
0.11	2.73	33.5	36	305	36	0.70	0.105	0.384	0.363
0.11	2.73	24.0	27	293	25	0.65	0.109	0.291	0.367
0.11	3.70	22.0	37	348	37	0.93	0.092	0.305	0.373
0.11	3.25	36.5	47	394	46	1.20	0.081	0.296	0.375
0.31	3.67	25.0	49	488	71	1.70	0.185	0.298	0.346
0.34	3.43	42.0	65	498	77	2.07	0.199	0.310	0.405
0.56	2.63	41.5	60	491	79	1.70	0.332	0.328	0.342
0.54	2.85	26.5	47	466	62	1.62	0.338	0.285	0.362
0.55	3.87	30.0	71	545	84	2.25	0.294	0.283	0.368
0.55	3.61	44.0	83	609	112	3.20	0.263	0.302	0.419
1.23	2.73	47.5	114	728	130	3.35	0.492	0.245	0.307
1.26	2.82	28.0	94	740	140	3.45	0.496	0.256	0.306

The thrust coefficient $K_T = T_A / 2\rho n_A^2 D^4$ and torque coefficient $K_Q = Q_A / 2\rho n_A^2 D^5$ in Tables 7 and 8 have been plotted versus the apparent advance coefficient $J_V = V / n_A D$ in Figure 6. In spite of the scatter in the data, to be expected because of intermittent ice-propeller interaction, the following equations could be fitted through the experimental results

$$K_T = 0.308 - 0.011 J_V - 0.167 J_V^2 \quad (6)$$

$$10 K_Q = 0.371 + 0.046 J_V - 0.248 J_V^2. \quad (7)$$

In Figure 7, the estimated total thrust delivered by the propellers has been plotted against the calculated total resistance in level ice at the self-propulsion points of the ship model. These values satisfy the linear regression

$$T_A = 1.25 R_{it} \quad (8a)$$

with a correlation $r = 0.96$. From eq 8a, the thrust deduction factor, $t = 1 - R_{it}/T_A$, in level ice was calculated as

$$t = 0.2. \quad (9a)$$

Figure 6. Thrust and torque coefficients in level ice versus apparent advance coefficient.

Figure 7. Model total thrust versus model total resistance in level ice at self-propulsion points.

The data points for the velocity of 0.11 m/s lie on the line $T_A = R_{it}$, indicating a thrust deduction factor of zero. It is more likely that the fluctuations in thrust and resistance measurements always present during ice tests did not permit determination of low values on t , on the order of 0.05 or less, such as were obtained in the low velocity tests in ice free conditions (Murdey 1980). The data obtained at velocities greater than 0.11 m/s yield

$$T_A = 1.285 R_{it} \quad (8b)$$

which corresponds to

$$t = 0.222. \quad (9b)$$

FULL-SCALE PERFORMANCE PREDICTIONS

Based on the above analysis of the model test data, full-scale performance of the CCGS R-class icebreaker is predicted as follows:

1. Under the Froude scaling law, the full-scale ice resistance is equal to λ^3 times the model resistance where λ is the geometric scale, equal to 20 in the present case. From the model resistance equation, eq 3, the full-scale ice resistance is given by

$$R_i = 359 h_i^2 + 68.4 v^{1.27} h_i^{1.37} + 3.21 \times 10^{-3} h_i^{0.3} \sigma^{1.7} \quad (10)$$

where R_i is expressed in kN, h_i in m, v in m/s and σ in kPa.

The total resistance is given by

$$R_{it} = R_i + R_{ow} \quad (11)$$

in which R_{ow} is obtained from the results of Murdey (1980).

a. $h_i = 0.7$ m, $\sigma = 800$ kPa.

b. $h_i = 0.45$ m, $\sigma = 800$ kPa.

Figure 8. Predicted full-scale performance.

2. A constant thrust deduction coefficient $t = 0.2$ is selected that is likely to be conservative at low velocity

$$T_A = 1.25 R_{it}. \quad (12)$$

3. The required propeller speed, n_A , in rpm is next calculated from eq 6, and the corresponding total torque from eq 7. The resulting delivered power is calculated by

$$P_{DI} = 2\pi \left(\frac{n_A}{60} \right) Q_A. \quad (13)$$

Calculations have been made for four conditions, namely: 1) $h_i = 0.70$ m, $\sigma = 800$ kPa; 2) $h_i = 0.45$ m, $\sigma = 800$ kPa; 3) $h_i = 0.70$ m, $\sigma = 400$ kPa, and 4) $h_i = 0.45$ m, $\sigma = 400$ kPa. The results are presented in Figure 8 and in Appendix A.

c. $h_i = 0.7$ m, $\sigma = 400$ kPa.

d. $h_i = 0.45$ m, $\sigma = 400$ kPa.

Figure 8 (cont'd).

COMPARISON WITH FULL-SCALE TRIAL DATA

A relatively complete set of full-scale measurements have been presented by Michailidis and Murdey (1981). The range of parameters V , h_i and σ of the full-scale trials were within that of the present model tests or nearly so. The primary difference was the presence of a snow cover that was not modeled in the laboratory tests. The presence of snow adds another component to the total resistance, namely the snow resistance R_s . Little is known about this resistance component. In a recent report, Carter (1983) assumed that R_s is proportional to the snow cover thickness h_s

$$R_s = k h_s \quad (14)$$

and suggested the value $k = 900$ when R_s is expressed in kN and h_s , the snow cover thickness, in m. For lack of better predictor, eq 14 with $k = 900$ was

Table 9. Calculated versus measured full-scale performance (field measurement from Michailidis and Murdey 1981).

V (m/s)	h_i (cm)	σ (kPa)	h_s (cm)	Calculated values					Field measurements		
				R_{it} (kN)	R_s (kN)	n_A (rpm)	T_A^* (kN)	PDI^{**} (kW)	n_A (rpm)	T_A^* (kN)	PDI^{**} (kW)
1.12	70.4	510	8.0	349	72	104	526	2913	119	578	3860
2.38	62.0	480	13.0	370	117	115	609	3773	127	648	4510
2.77	67.4	460	9.0	436	81	119	647	4172	133	707	5510
2.08	67.6	460	15.0	381	135	117	645	4057	145	826	7450
3.63	65.0	460	11.0	495	99	130	742	5250	155	917	8020
4.23	66.6	460	12.0	571	108	140	848	6489	172	1056	10900
3.93	61.3	460	9.0	489	81	128	712	5002	164	957	9190
1.82	73.8	300	52.0	355	468	146	1028	8012	164	1177	10950
0.99	75.4	300	48.0	303	432	137	919	6651	154	1094	9540
0.80	88.3	300	50.0	377	450	145	1033	7894	144	980	7900

*Total thrust.

**Total delivered power.

adopted here in the calculation of the predicted total resistance of the CCGS R-class icebreaker for the full-scale trial conditions of velocity, ice thickness and strength, and snow cover thickness. The total resistance in snow covered ice is thus given by

$$R_T = R_I + R_{ow} + k h_s. \quad (15)$$

The corresponding rpm, thrust and delivered power were calculated following steps 2 and 3 of the preceding section. The results of the calculations are listed in Table 9 together with the measured values from Michailidis and Murdey (1981), and are compared against the latter in Figure 9. As can be seen, the calculated values for the propeller speed, thrust and delivered power are consistently lower than the measured ones by an average of 13.1, 14.4 and 28.8% respectively.

An indirect check of the validity of the model test results can be made by calculating the thrust and power delivered by the propellers for the full-

Figure 9. Predicted versus measured full-scale performance (a - propeller speed, b - total thrust and power).

Table 10. Calculated and measured thrust and power at full-scale speed and propeller rpm.

V (m/s)	n_A (rpm)	Measured thrust (kN)	Calculated thrust (kN)	Measured power (MW)	Calculated power (MW)
1.12	119.0	578	688	3.86	4.34
2.39	126.7	648	751	4.51	5.12
2.77	133.3	707	823	5.51	5.92
2.08	144.5	827	997	7.45	7.70
3.63	155.2	917	1098	8.02	9.24
4.23	172.0	1056	1339	10.09	12.51
3.93	163.5	957	1214	9.19	10.77
1.82	163.8	1177	1296	10.95	11.29
0.99	153.5	1094	1152	9.54	9.32
0.80	143.6	980	1009	7.90	7.62

scale values of ship velocity and propeller rpm and comparing the results with the measured full-scale values. The results of these calculations are presented in Table 10 and Figure 10. The calculated thrust and power are now somewhat higher than the measured values by an average of 13.7% for the thrust and only 7.7% for the power. These latter results, especially the very good agreement between measured and calculated power, indicate that the propeller characteristics represented by the relationships between advance coefficient J and thrust and torque coefficients, K_T and K_Q (eq 6 and 7 respectively), were satisfactorily duplicated in the model tests.

The sizable discrepancy between the measured thrust, rpm and, especially, delivered power and their calculated values based on the ice resistance predicted by eq 15, 14 and 10 may be attributed to several factors: 1) eq 10 predicts too low an ice resistance R_i , 2) the thrust deduction coefficient value of $t = 0.2$ deduced from the model test results is incorrect, 3) the assumed coefficient $k = 900$ in eq 14 for the calculation of R_s is incorrect, and 4) a combination of the three above factors.

Figure 10. Calculated versus measured thrust and power at full-scale speed and propeller rpm.

Let us assume for the time being that the ice resistance given by eq 10 is indeed correct, and that the main sources of disagreement are erroneous values of k and t . A regression analysis of the measured values of T_A versus the calculated R_{it} and measured snow thickness according to the equation

$$T_A = \frac{R_{it} + k h_s}{1 - t} \quad (16)$$

yielded values of

$$k = 661 \text{ kN/m}$$

$$t = 0.37$$

with a correlation factor of 0.914. While the value of k may be valid, a thrust deduction coefficient of 0.37 is unrealistically high. This writer is of the opinion that the discrepancy between the measured and calculated values of thrust, rpm and particularly power arises primarily from an underestimation of the ice resistance R_i by eq 10. This underestimation of R_i is likely from too low a friction factor of the model as compared to that of the full-scale ship. As stated earlier, the model friction coefficient was measured at 0.04. That of the ship was not measured during the trials reported by Michailidis and Murdey (1981), but Edwards et al. (1981), who describe full-scale trials of a sister ship, reported that the ice-hull friction coefficient was equal to 0.30 at low speed and 0.19 at high speed. Additional model tests at an ice-hull friction factor f of the order of 0.2 would be needed to determine the effect of f on the coefficients of eq 10 and to verify the above contention. Because the full-scale trials reported by Edwards et al. (1981) were conducted at a lower draft of 6.08 m -- with corresponding changes in beam and length at waterline, wetted surface area and displacement -- than the present model tests, comparison of these trials' results with the predictions from the model tests would be invalid.

SUMMARY AND CONCLUSIONS

1. Resistance and propulsion tests were made on a 1:20-scale model of the latest Canadian Coast Guard R-class icebreaker. Resistance tests were made in level ice and in precut ice, and a resistance equation was derived.

Propulsion tests were made in level ice only. These tests gave an average value of 0.20 for the thrust deduction factor. Relationships between the thrust and torque coefficients, K_T and K_Q , and the apparent advance coefficient J_v were established.

2. From the model tests, an equation for the full-scale resistance in level ice was established, and self-propulsion characteristics for the four sets of ice conditions prescribed by the ITTC committee were calculated.

3. Comparison between predicted ship performance and available full-scale trial measurements was attempted. This required an assumption of the additional resistance from the snow cover on the ice.

The predicted propeller rpm, thrust and especially delivered power based on the resistance equation derived from the test results were significantly lower than the corresponding measured values. On the other hand, the predicted thrust and power calculated for the measured full-scale values of ship speed and propeller rpm were somewhat higher but in much better agreement with those measured during the field trials.

It was concluded that the ice resistance was underestimated in the model tests as compared to that of the full-scale ship primarily because the model had a much lower ice-hull friction coefficient. It would therefore be desirable to repeat the model tests with a higher model friction coefficient on the order of 0.2 as compared to its value of 0.04 in the present tests.

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APPENDIX A: PREDICTED FULL-SCALE PERFORMANCE.

V (m/s)	R _{it} (kN)	n _A (rpm)	T _A * (kN)	Q _A † (kNm)	P _{DI} ** (kW)
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$h_i = 0.70 \text{ m}, \sigma = 800 \text{ kPa}$

0.00	424	104	530	132	2860
0.25	432	105	540	135	2955
0.50	443	106	554	139	3091
0.75	456	108	570	144	3252
1.00	471	110	589	149	3435
1.25	488	112	609	155	3639
1.50	505	115	631	161	3862
1.75	524	117	655	167	4106
2.00	543	120	679	174	4368
2.25	564	123	705	181	4650
2.50	586	125	732	189	4952
2.75	608	128	760	196	5273
3.00	631	131	789	204	5615
3.25	656	134	819	212	5976
3.50	680	138	851	221	6358
3.75	706	141	883	229	6761
4.00	733	144	916	238	7185
4.25	760	147	950	248	7630
4.50	787	150	984	257	8097
4.75	816	154	1020	266	8586
5.00	845	157	1056	276	9097
5.25	875	161	1094	286	9631
5.50	905	164	1132	297	10188
5.75	936	167	1171	307	10769
6.00	968	171	1210	318	11373

$h_i = 0.45 \text{ m}, \sigma = 800 \text{ kPa}$

0.00	290	86	363	90	1618
0.25	295	87	368	92	1667
0.50	301	88	376	95	1736
0.75	309	89	386	98	1820
1.00	318	91	398	101	1917
1.25	328	93	410	105	2025
1.50	339	94	424	108	2146
1.75	351	97	438	113	2278
2.00	363	99	454	117	2422
2.25	376	101	471	122	2578
2.50	390	104	488	126	2746
2.75	405	106	506	131	2926
3.00	420	109	525	137	3118
3.25	436	112	545	142	3324
3.50	453	114	566	148	3542
3.75	470	117	587	154	3774
4.00	487	120	609	160	4019
4.25	506	123	632	166	4278
4.50	524	126	656	172	4551
4.75	544	129	680	179	4838
5.00	564	132	705	185	5140
5.25	584	135	730	192	5457
5.50	605	139	756	199	5789
5.75	626	142	783	207	6137
6.00	648	145	810	214	6501

V (m/s)	R _{it} (kN)	n _A (rpm)	T _A [*] (kN)	Q _A [†] (kNm)	P _{DI} ^{**} (kW)
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$h_i = 0.70 \text{ m}, \sigma = 400 \text{ kPa.}$

0.00	252	80	316	78	1312
0.25	260	81	325	81	1383
0.50	271	83	339	85	1485
0.75	284	85	356	90	1609
1.00	299	88	374	95	1752
1.25	316	91	394	101	1913
1.50	333	94	416	107	2091
1.75	352	97	440	113	2288
2.00	371	100	464	120	2502
2.25	392	103	490	127	2735
2.50	414	107	517	134	2986
2.75	436	110	545	141	3256
3.00	460	113	574	149	3545
3.25	484	117	605	157	3854
3.50	509	121	636	166	4183
3.75	534	124	668	174	4532
4.00	561	128	701	183	4901
4.25	588	131	735	192	5292
4.50	616	135	769	202	5704
4.75	644	139	805	211	6138
5.00	673	143	842	221	6594
5.25	703	146	879	231	7073
5.50	733	150	917	241	7574
5.75	765	154	956	251	8099
6.00	796	158	995	262	8647

$h_i = 0.45 \text{ m}, \sigma = 400 \text{ kPa.}$

0.00	140	60	175	43	540
0.25	144	61	180	45	571
0.50	151	62	188	47	618
0.75	158	64	198	50	675
1.00	167	66	209	53	743
1.25	177	69	222	57	820
1.50	188	71	235	61	908
1.75	200	74	250	65	1005
2.00	213	77	266	69	1113
2.25	226	80	282	74	1232
2.50	240	83	300	78	1362
2.75	254	86	318	83	1503
3.00	270	90	337	88	1656
3.25	286	93	357	94	1821
3.50	302	96	378	99	1999
3.75	319	100	399	105	2189
4.00	337	103	421	111	2392
4.25	355	106	444	117	2609
4.50	374	110	467	123	2839
4.75	393	113	492	130	3083
5.00	413	117	516	137	3342
5.25	433	120	542	143	3615
5.50	454	124	568	150	3903
5.75	476	127	595	158	4207
6.00	498	131	622	165	4526

*Total thrust.

†Torque per propeller.

**Total delivered power.